# Population III binary population synthesis 

International Teeminar<br>Speaker: Ataru Tanikawa ${ }^{1}$

Collaborators: Kinugawa T. ${ }^{1}$, Hijikawa, K. ${ }^{1}$, Susa H. ${ }^{2}$, Takahashi K. ${ }^{3}$, Trani A. A. ${ }^{1}$, Umeda H. ${ }^{1}$, Yoshida T. ${ }^{4}$ Institutes:
${ }^{1}$ The University of Tokyo, ${ }^{2}$ Konan University, ${ }^{3}$ Max
Planck Institute, ${ }^{4}$ Kyoto University

## About me



## About me



- $\Delta$ tam Tanikavia


- Tanikawa (2018, ApJ, 858, 26) Its of wnıte Tanikawa, Giersz, Arca Sedda intermediate mass BH
(2021, arXiv:2103.14185)


## Contents

- Gravitational wave (GW) observations and black hole (BH) mergers
- Fitting formulae of extremely metal poor (EMP) stars and very massive stars
- BH mergers from Population (Pop) III stars
- The pair instability (PI) mass-gap event GW190521


## Gravitational wave (GW)

GW150914 (Abbott et al. 2016)

- The first detection of GWs is the first discovery of a BH merger 2015.
- The number of $\mathrm{BH}-\mathrm{BH}$ g grows to $\sim 50$ only during 5 years.
- The origin of BH mergers

- Isolated binary stars?
- Multiple star systems?
- Dense star clusters?
- More than one channel?




## Binary population synthesis and star cluster simulation

- Binary population synthesis and star cluster simulation are very powerful to predict properties of BH mergers.
- Single star evolution has to be followed in parallel with binary interaction and cluster evolution.
- Usually, the single star evolution is followed with
- Fitting formulae
- Lookup table
- Not hydrodynamic simulation due to the high calculation cost


Pop III very massive binary stars


Hijikawa, AT et al. (2021, MNRAS in press)

Belczynski et al. (2020)


# Fitting formulas (FFs) of EMP stars and very massive stars 

## FFs for single star evolution

- Single-Star Evolution (SSE) (Hurley et al. 2000)
- Fitting formulae for stars with
$M=0.5-50 M_{\odot}$ and
$Z=0.0001-0.03$
- Extended to $M \sim 1000 M_{\odot}$
- Coupled with
- Binary population synthesis codes: BSE, MOBSE, StarTrack, COSMIC, ...
- Star cluster simulation codes: NBODY6++GPU, MOCCA, PeTar, CMC...


Hurley et al. (2000)

## Our FFs

- Extensions
- To EMP stars with $Z=10^{-8} Z_{\odot}$, identical to $Z=0 Z_{\odot}$ stars
- To very massive stars with $M=1280 M_{\odot}$ for $Z=10^{-8} Z_{\odot}$ and $Z=10^{-2}-10^{-1} Z_{\odot}$
- Support for
- BSE (e.g. Tanikawa et al. 2021, ApJ, 910, 30; Tanikawa et al. 2021, MNRAS in press, Hijikawa, AT et al. 2021, MNRAS in press)
- MOCCA ... incorporated.
- NBODY6++GPU and PeTar ... I'm happy to incorporate.


## Reasons for EMP FFs

- Difficult to reproduce EMP star evolution by the FF of the most metal-poor stars in SSE
$\left(Z=10^{-4}\right)$
- $Z=2 \times 10^{-10}$ stars
- No Hertzsprung-gap (HG)
$\rightarrow$ Common envelope (CE) becomes easier to succeed.
- No red supergiants for $10 M_{\odot} \lesssim M \lesssim 50 M_{\odot}$
$\rightarrow$ Mass transfer (MT) becomes more stable (or avoids CE).



## Overview of our FFs

- HG gradually appears with metallicity increasing.
- Red supergiant range becomes wider with metallicity increasing.
- $Z=2 \times 10^{-4}$ star models look similar between original SSE and our FFs.
- Not the same, because of different simulation data
- $Z=2 \times 10^{-3}$ star models are also supported.

Tanikawa et al. (2020, MNRAS, 495, 4170)


## BH mergers from Pop III stars

## Pop III stars

## (First and metal-free stars)

- Consisting of primordial gas (mostly H and He )
- Born in the high-redshift universe
- Astrophysical importance: stellar nucleosynthesis, reionization, ...
- Top-heavy initial mass function (IMF) predicted theoretically (Omukai, Nishi 1998; Abel et al. 2002; Bromm, \& Larson 2004)
- Not yet discovered (Frebel, Norris 2015 for review)
- Detectability of GWs from Pop III BH mergers



Greif et al. (2012)

## Pop III BH mergers

- $\sim 30 M_{\odot}$ peak in BH mergers
- A few $10 M_{\odot}$ Pop III stars end with blue supergiants.
- Blue supergiants tend to experience stable MT, not CE.
- Top-heavy IMF
- Possibly many $>100 M_{\odot}$ Pop III stars
- IMBH mergers?
- But, ...
- Pop III formation rate may be too small (Hartwig et al. 2016; Belczynski et al. 2017)
- Pop III binary stars might be only wide.



## Pop III binary stars

- Pop III single stars expand up to
$\sim 100 R_{\odot}$ in protostar phases due to high mass accretion.
- Pop III stars may not form short-period binary stars with $a \lesssim 100 R_{\odot}$.
- But, ...
- Pop III binary stars may be formed after protostar phases.
- Mass accretion is different between Pop III single and binary stars
- Two cases
- With short-period binaries
- Without short-period binaries


Hosokawa \& Omukai (2009)

## Initial conditions

- Instantaneous formation of Pop III stars: $\sim 10^{13} M_{\odot} \mathrm{Gpc}^{-3}$ at $z \sim 10$
- Consistent with numerically predicted results (Magg et al. 2016; Skinner, Wise 2020; but see Inayoshi et al. 2021)
- Binary fraction: 1 (e.g. Sugimura et al. 2020)
- Primary IMF: $f\left(m_{1}\right) \propto m_{1}^{-1}\left(10 M_{\odot} \leq m_{1} \leq 300 M_{\odot}\right)$
- Mass ratio: $f(q) \propto$ const $\left(10 M_{\odot} / m_{1} \leq q \leq 1\right)$
- Semi-major axis: $f(a) \propto a^{-1}\left(a_{\min } \leq a \leq 2000 R_{\odot}\right)$
- $a_{\text {min }}=10 R_{\odot}$ or $200 R_{\odot}$


Hirano et al. (2015)

- Eccentricity: $f(e) \propto e$


## Numerical setup

- Tanikawa's FF with $Z=10^{-8} Z_{\odot}$
- No stellar wind
- Fryer's rapid model for supernova with pair instability (PI) model like the strong PI of Belczynski et al. (2020).
- No natal kick
- Stellar envelope property in Post-MS phases
- Radiative: $\log \left(T_{\text {eff }}\right)>3.65$
- CHeB phase in the original BSE
- Convective: $\log \left(T_{\text {eff }}\right)<3.65$
- AGB phase in the original BSE


Convective (red supergiants)


## 

- The merger rate density is $\sim 0.1 \mathrm{yr}^{-1} \mathrm{Gpc}^{-3}$ regardless of $a_{\text {min }}$.
- Much smaller than the observed rate ( $\sim 10 \mathrm{yr}^{-1} \mathrm{Gpc}^{-3}$ ).
- The $30 M_{\odot}$ peak disappears for $a_{\text {min }}=200 R_{\odot}$
- The stable MT channel needs short-period binaries.

optiq0.0ale1
$t_{\mathrm{d}}=10-15 \mathrm{Gyr}$



- The PI mass gap $50-130 M_{\odot}$
- The merger rate density of IMBH mergers (IMBH-IMBH or IMBH-BH) is
$\sim 0.01 \mathrm{yr}^{-1} \mathrm{Gpc}^{-3}$ regardless of $a_{\mathrm{min}}$.
- Not violate the upper limit of
$\sim 0.056 \mathrm{yr}^{-1} \mathrm{Gpc}^{-3}$ (LVK, arXiv: 2105.15120)
- Detectable soon if our model is correct

Tanikawa et al. (2021, ApJ, 910, 30)


## The PI mass-gap event GW190521

## GW190521

- Merger of $85_{-14}^{+21} M_{\odot}$ and $66_{-18}^{+17} M_{\odot}$ BHs
- The primary BH has only a $0.32 \%$ probability of being below $65 M_{\odot}$.
- At least one BH lies within the PI mass gap.
- Possible scenarios
- Cluster origins (Rodriguez et al. 2019; Di Carlo et al. 2020; Tagawa et al. 2020; Fragione et al. 2020; Rizzuto et al. 2021)
- Uncertainty of PI mass gap boundary (Farmer et al. 2020; Belczynski et al. 2020; Costa et al. 2021)
- Uncertainty of convective overshoot


TABLE I. Parameters of GW190521 according to the
NRSur7dq4 waveform model. We quote median values with $90 \%$ credible intervals that include statistical errors.

| Parameter |  |
| :---: | :---: |
| Primary mass | ${ }^{85}{ }_{-14}^{+21} M_{\odot}$ |
| Secondary mass | $66_{-18}^{+17} M_{\odot}$ |
| Primary spin magnitude | $0.699_{-0.62}^{+0.27}$ |
| Secondary spin magnitude | $0.73{ }_{-0.64}^{+0.24}$ |
| Total mass | $150_{-17}^{+29} M_{\odot}$ |
| Mass ratio ( $m_{2} / m_{1} \leq 1$ ) | 0.79 ${ }_{-0.29}^{+0.19}$ |
| Effective inspiral spin parameter ( $\chi_{\text {eff }}$ ) | $0.08_{-0.36}^{+0.27}$ |
| Effective precession spin parameter ( $\chi_{\mathrm{p}}$ ) | $0.688_{-0.37}^{+0.25}$ |
| Luminosity Distance | $5.3{ }_{-2.6}^{+2.4} \mathrm{Gpc}$ |
| Redshift | $0.822_{-0.34}^{+0.28}$ |
| Final mass | $142_{-16}^{+28} M_{\odot}$ |
| Final spin | $0.72_{-0.12}^{+0.09}$ |
| $P\left(m_{1}<65 M_{\odot}\right)$ | 0.32\% |
| $\log _{10}$ Bayes factor for orbital precession | $1.06{ }_{-0.06}^{+0.06}$ |
| $\log _{10}$ Bayes factor for nonzero spins | $0.922_{-0.06}^{+0.06}$ |
| $\log _{10}$ Bayes factor for higher harmonics | $-0.38_{-0.06}^{+0.06}$ |



Abbott et al. (2021)

Abbott et al. (2020)

## Revisit of the PI mass gap

## Single star evolution





Spera, Mapelli (2017)

Belczynski et al. (2016)

Binary star evolution


## Reconsider Pop III model

Yoshida et al. (2019)

- No massive Pop. III stars discovered so far
- Extrapolation from nearby stars to Pop. III stars
- L model: the same as before, similar to Stern (Brott et al. 2011)
- M model: similar to GENEC (Ekstrom et al. 2012; Farrell et al. 2020)
- The maximums radius of a $80 M_{\odot}$ star
- M model: $\sim 40 R_{\odot}$, similar to Farrell et al. (2020)
- L model: $\sim 3 \times 10^{3} R_{\odot}$, similar to Yoon et al. (2012)
- Similar issue is also discussed by Vink et al. (2021)




## Convective overshoot

- More effective overshoot
- Larger He core at the end of MS
- Larger luminosity in post-MS
- Larger radius in post-MS

- Effectiveness of overshoot
- M model: less effective overshoot
- L model: more effective overshoot

Both consistent with Pop I/II stars


## Binary population synthesis

- FFs
- L model, the same as previous Pop III ones
- M model, the smaller overshoot
- Initial conditions

- $f\left(m_{1}\right) \propto m_{1}^{-1}$

$$
\left(10 M_{\odot} \leq m_{1} \leq 150 M_{\odot}\right)
$$

- $f(a) \propto a^{-1}$
$\left(10 R_{\odot} \leq m_{1} \leq 2000 R_{\odot}\right)$



## BH mass distribution

- M model
- The maximum mass: $\sim 100 M_{\odot}$
- Stars lose little mass through binary interactions.
- Pop. III stars can form GW190521-like BH-BHs.
- L model
- The maximum mass: $\sim 50 M_{\odot}$
- Stars lose their H envelopes through binary interactions
- No Pop. III stars can form GW190521-like BH-BHs.


## Pop III stars can form the PI mass-gap

 event if overshoot is ineffective.

Tanikawa et al. (2021, MNRAS in press)

## Difference from cluster origin

- Even if the M model is correct, no Pop. III binary can form BH-BHs with $100-130 M_{\odot}$.
- If GW190521 is Pop. III, the merger rate of $\mathrm{BH}-\mathrm{BHs}$ with $100-130 M_{\odot}$ is much smaller than with $50-100 M_{\odot}$.




## Summary

- The origins of BH mergers have been under debate.
- We have extended BSE to EMP stars and very massive stars.
- We have investigated Pop III BH mergers.
- $\sim 30 M_{\odot}$ peak can disappear if Pop III binary stars are only long-period.
- Pop III IMBH merger rate can be $\sim 0.01 \mathrm{yr}^{-1} \mathrm{Gpc}^{-3}$, which may be detected in the near future.
- Pop III stars can form the PI mass-gap event GW190521 if convective overshoot is not effective.

