

Theoretical study of the origins of merging binary black holes

Colloquium 2021/06/14

Astronomical Institute, Tohoku University

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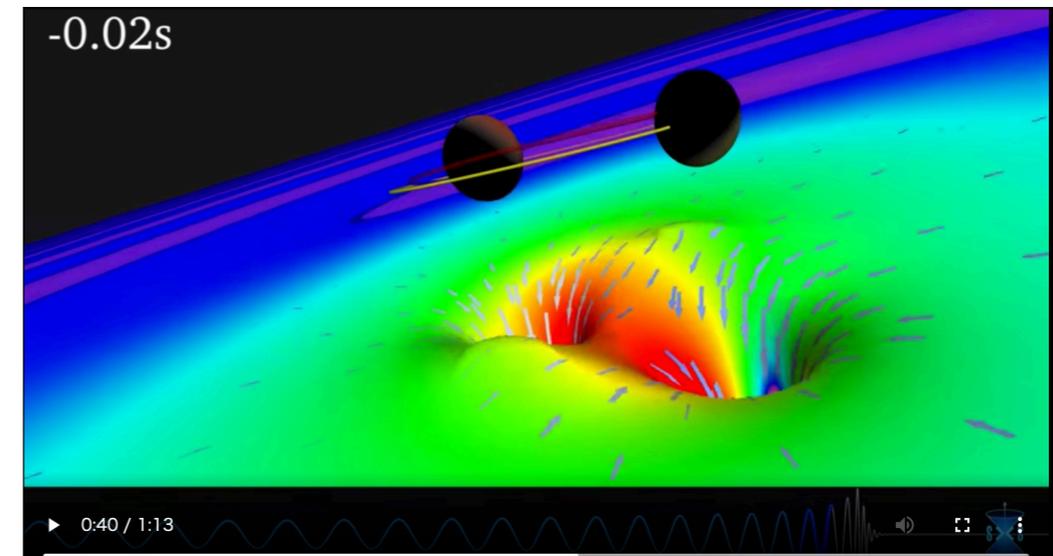
Contents

- Gravitational wave (GW) observations and stellar-mass black hole (BH) mergers
- Merging binary BHs formed in open clusters
- Formation scenario of the pair instability (PI) mass gap event GW190521

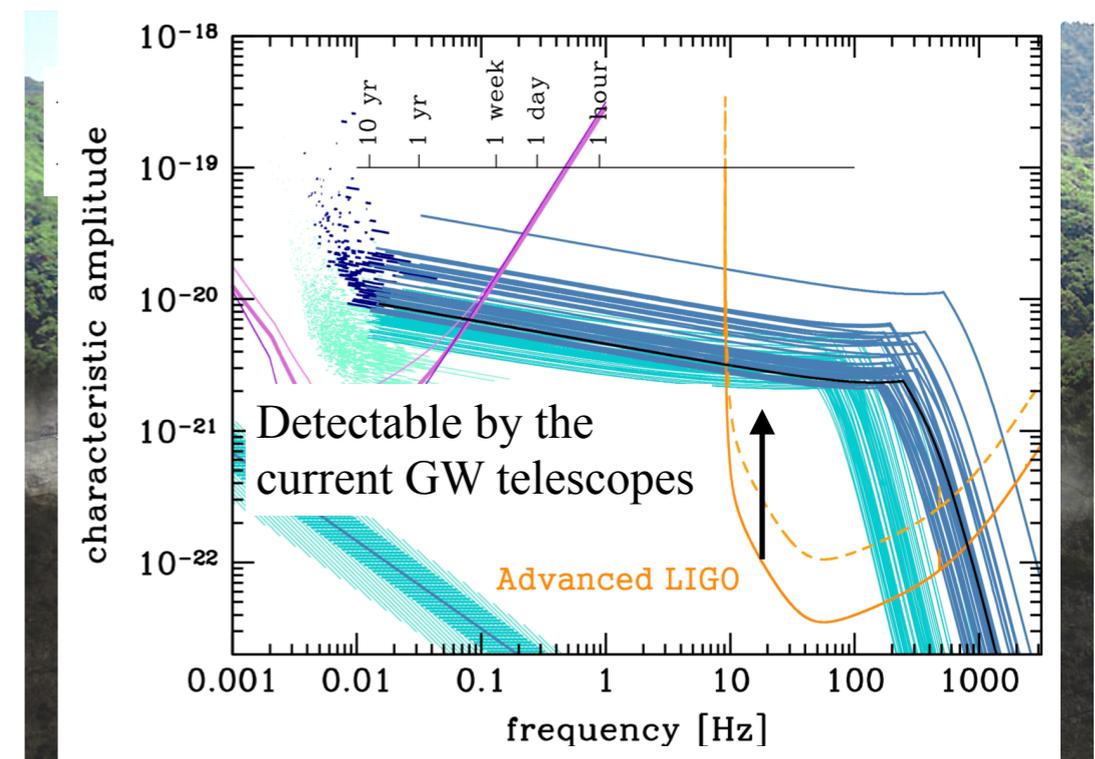
GWs from BH mergers

- A life of a merging binary BH
 - Born as BH-BH with masses of $\sim 10M_{\odot}$ and separation of $\lesssim 100R_{\odot} \lesssim 10$ Gyr ago
 - Shrink the separation through GW radiation, **not detectable**
 - Large GW emission $\lesssim 1$ sec before their merger, **detected by GW telescopes**
- GW telescopes sensitive to 10-1000Hz

$$f_{\text{gw}} \sim \frac{1}{P(r_{\text{sch}})} \sim 10^2 \text{ Hz} \left(\frac{M_{\text{BH-BH}}}{10^2 M_{\odot}} \right)^{-1}$$



SXS project

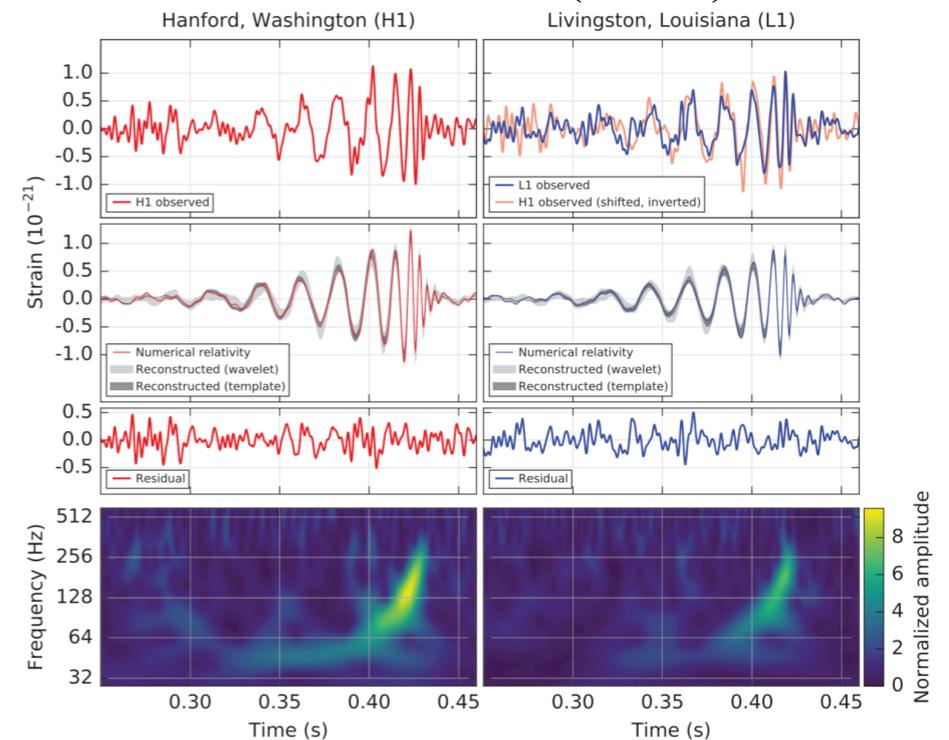


Sesana (2016)

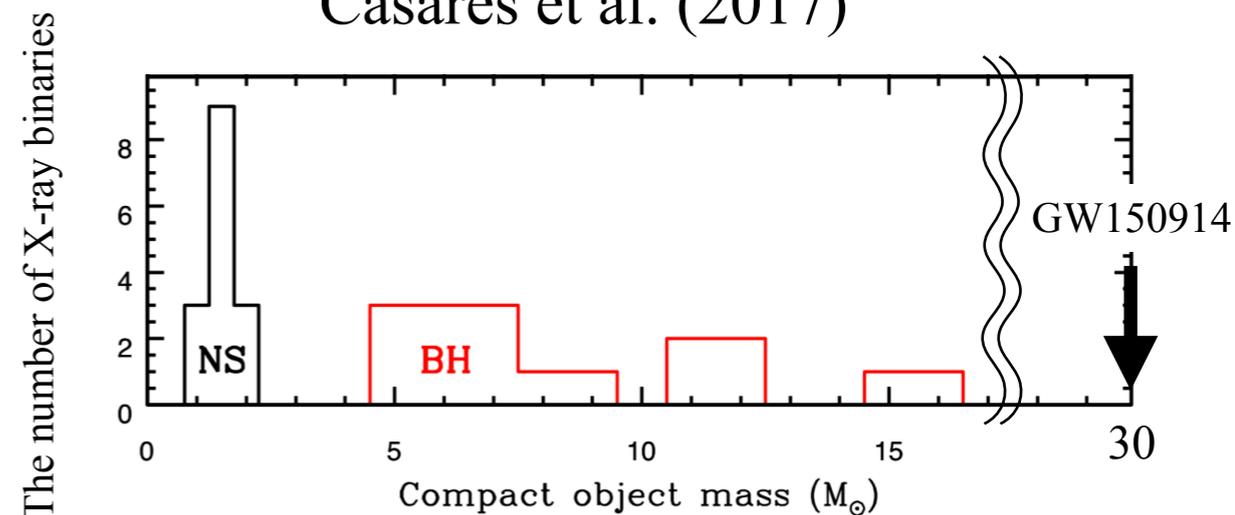
The first detection: GW150914

- Detected on 14 September 2015
- Merger of $36M_{\odot}$ and $29M_{\odot}$ BHs
- BHs heavier than observed before
 - Metal-poor star?
 - Star clusters?
 - Primordial BH?
- Compact binary BH
 - Merger time: $\lesssim 10^{10}$ yr
 - Separation: $\lesssim 10^2 R_{\odot}$ at the formation of the binary BH.
 - Red supergiants: $\gtrsim 10^3 R_{\odot}$

Abbott et al. (2016)



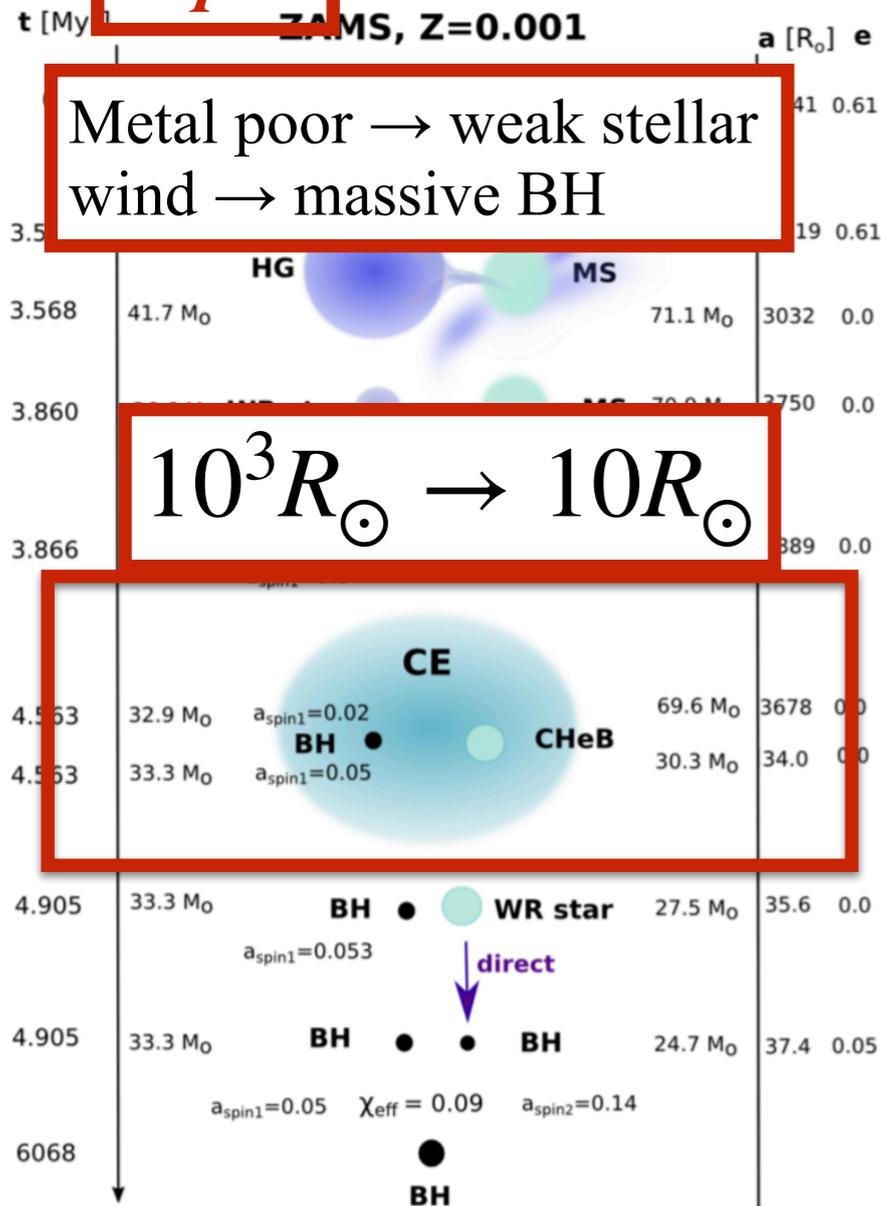
Casares et al. (2017)



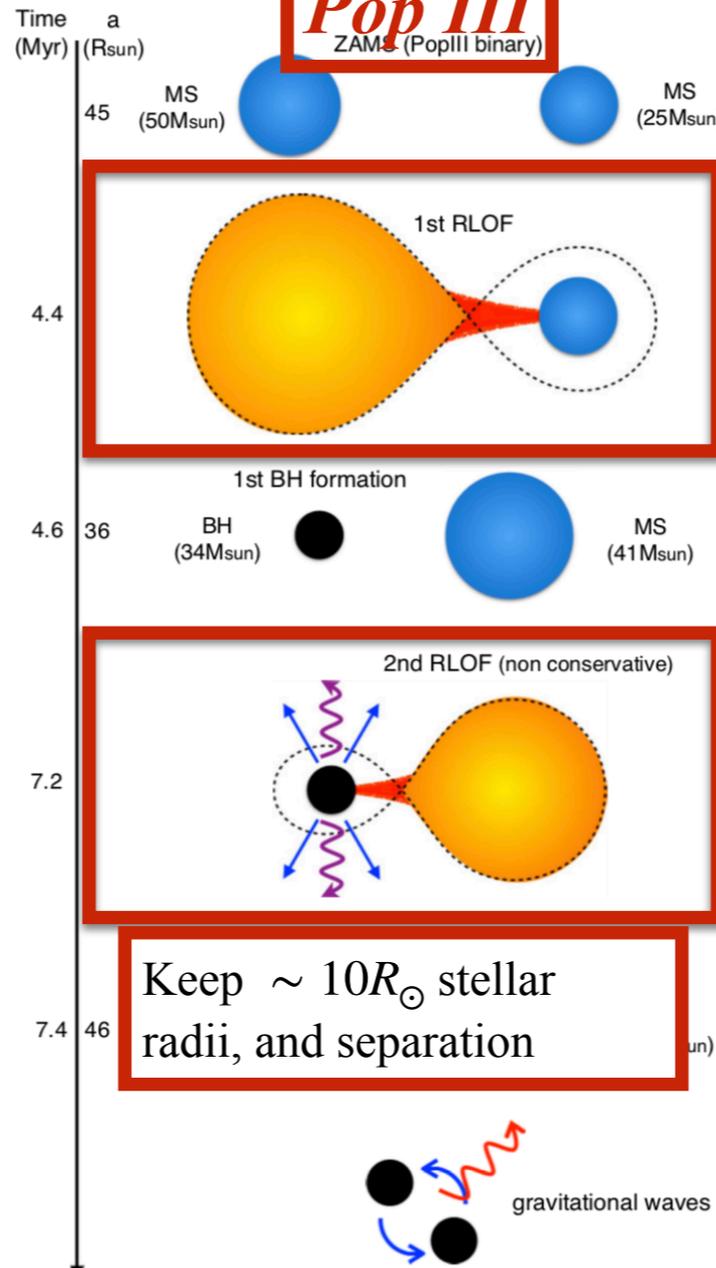
Many formation scenarios

Isolated binary stars

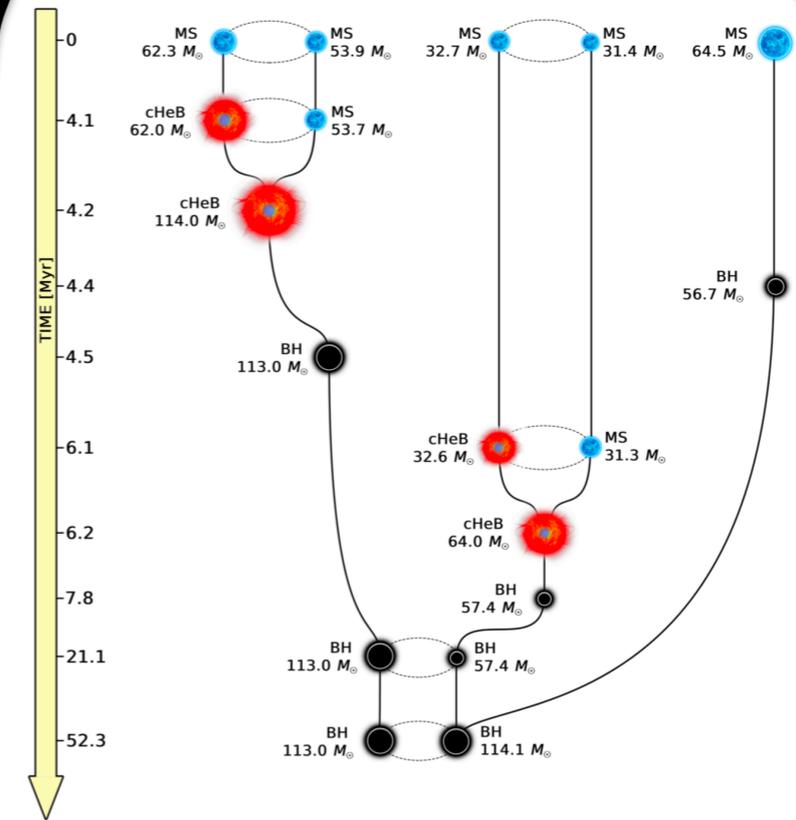
Pop II



Pop III



Star cluster

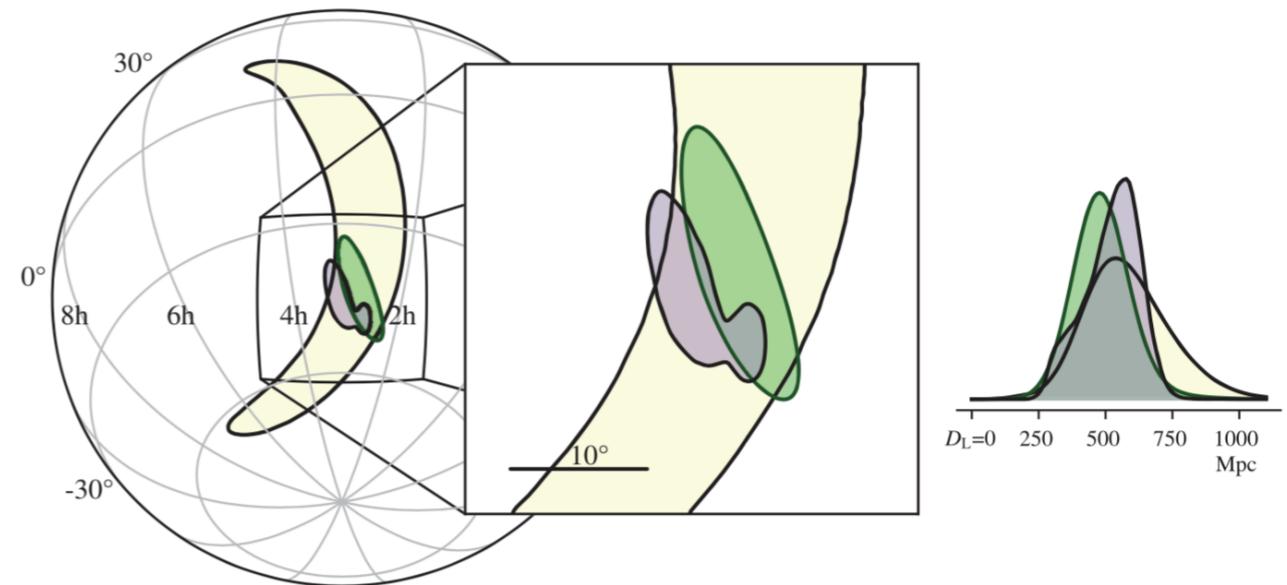


- Metal poor, and repeated BH mergers
- $\infty \rightarrow 10 R_{\odot}$ after BH formation

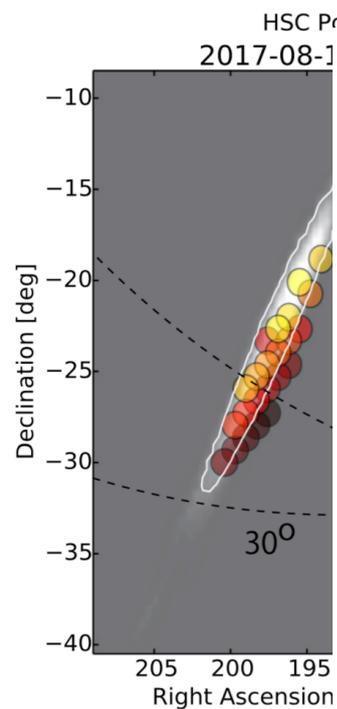
Difficulty of identification

- Large sky localization
- Impossible to find the host galaxy
- No conclusive electromagnetic counterpart unlike NS mergers

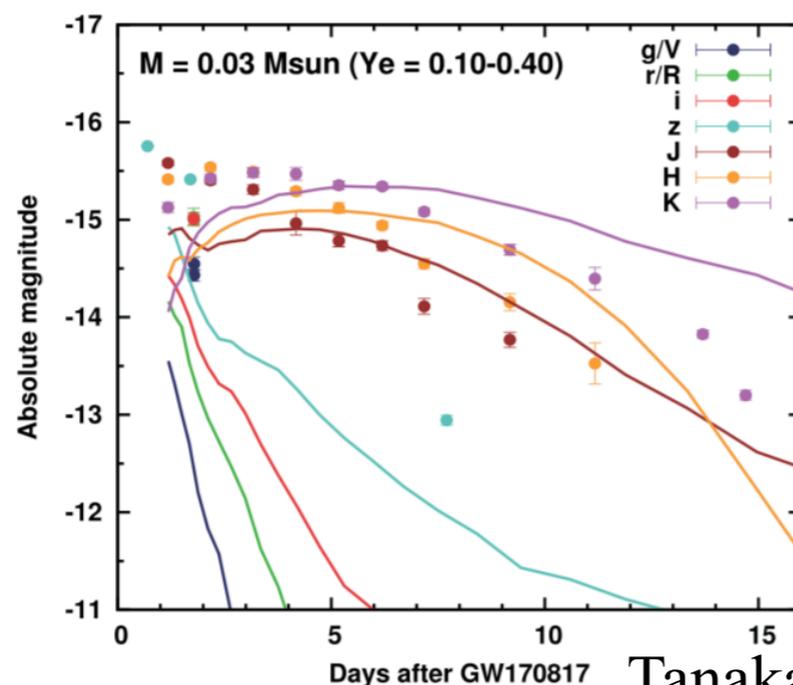
GW170814 (Abbott et al. 2017)



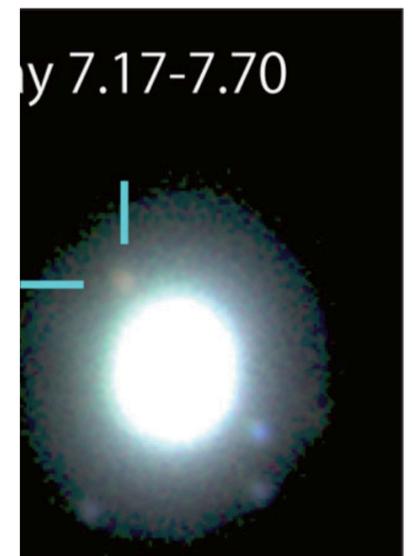
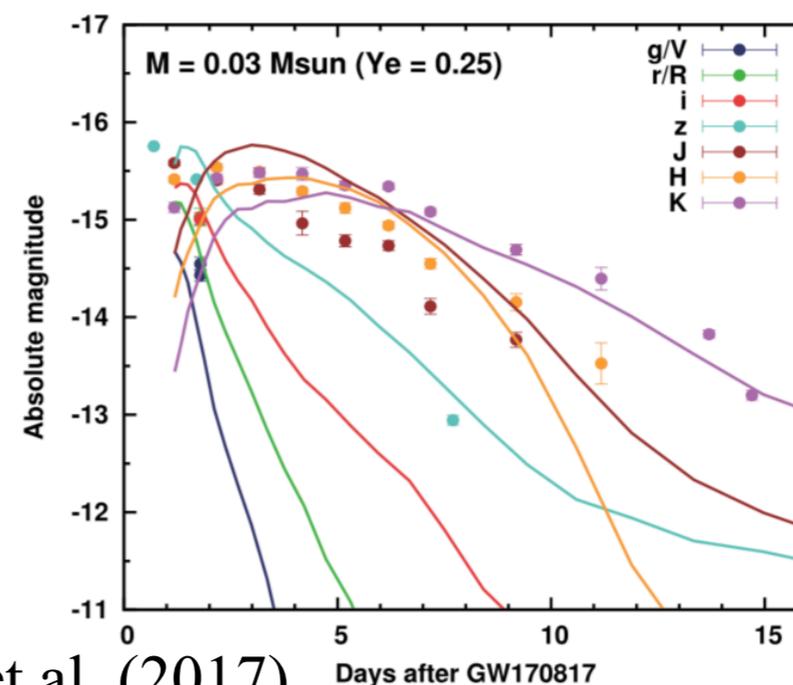
GW170817, NS merger



Tomihaga et al. (2016)



Tanaka et al. (2017)



7)

Clues for identification

- BH merger rate density: R [$\text{yr}^{-1} \text{Gpc}^{-3}$]
- Primary BH mass: m_1 [M_\odot]
- Secondary BH mass: m_2 [M_\odot]
 - Mass ratio: $q = m_2/m_1$

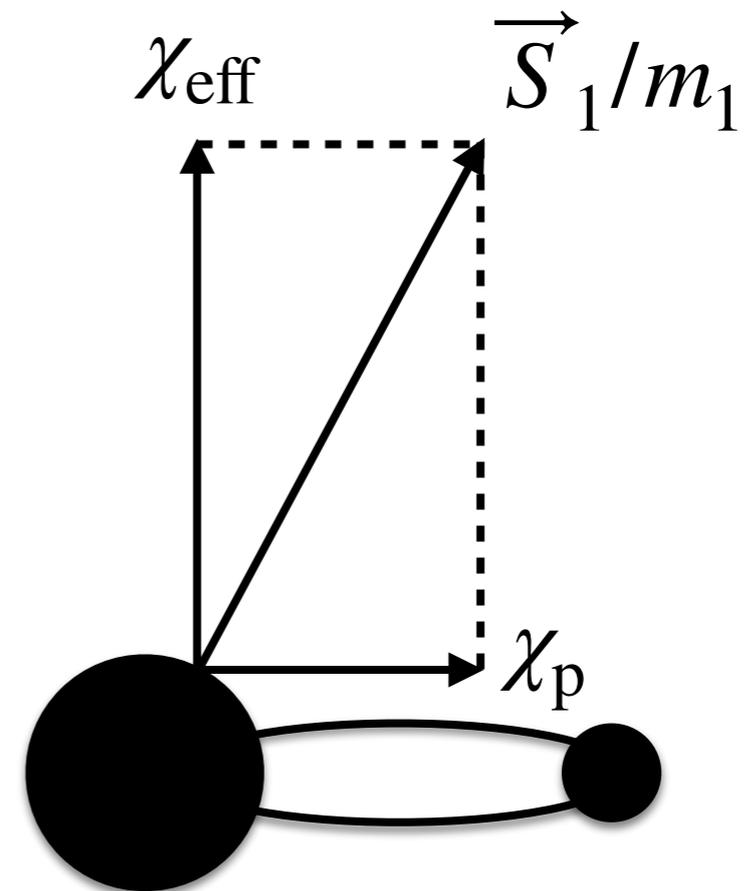
- Effective spin: χ_{eff}

$$\chi_{\text{eff}} = \frac{1}{m_1 + m_2} \left(\frac{S_{1,\parallel}}{m_1} + \frac{S_{2,\parallel}}{m_2} \right)$$

- Spin precession: χ_p

$$\chi_p = \max \left(\frac{S_{1,\perp}}{m_1^2}, \frac{S_{2,\perp}}{m_2^2} \kappa(q) \right)$$

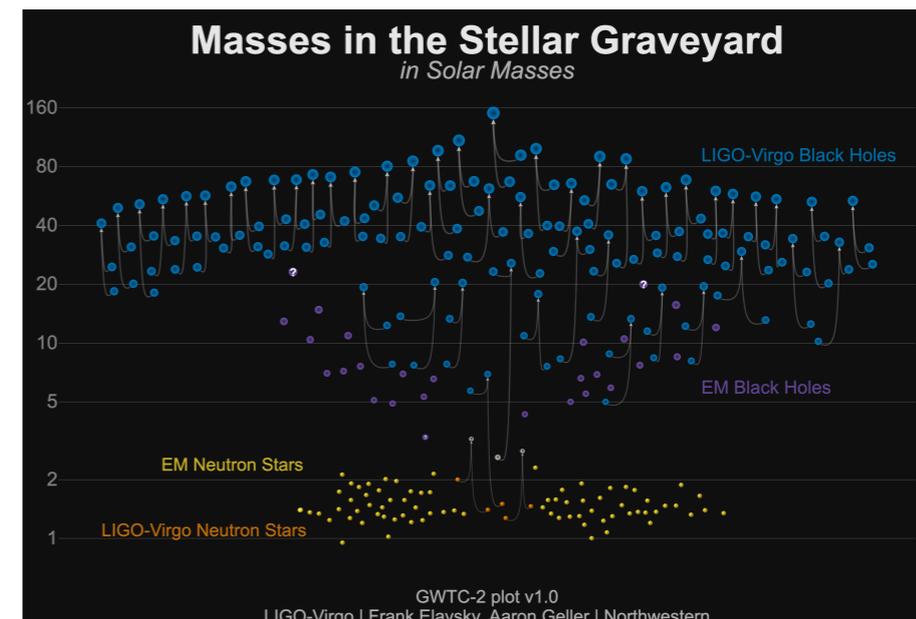
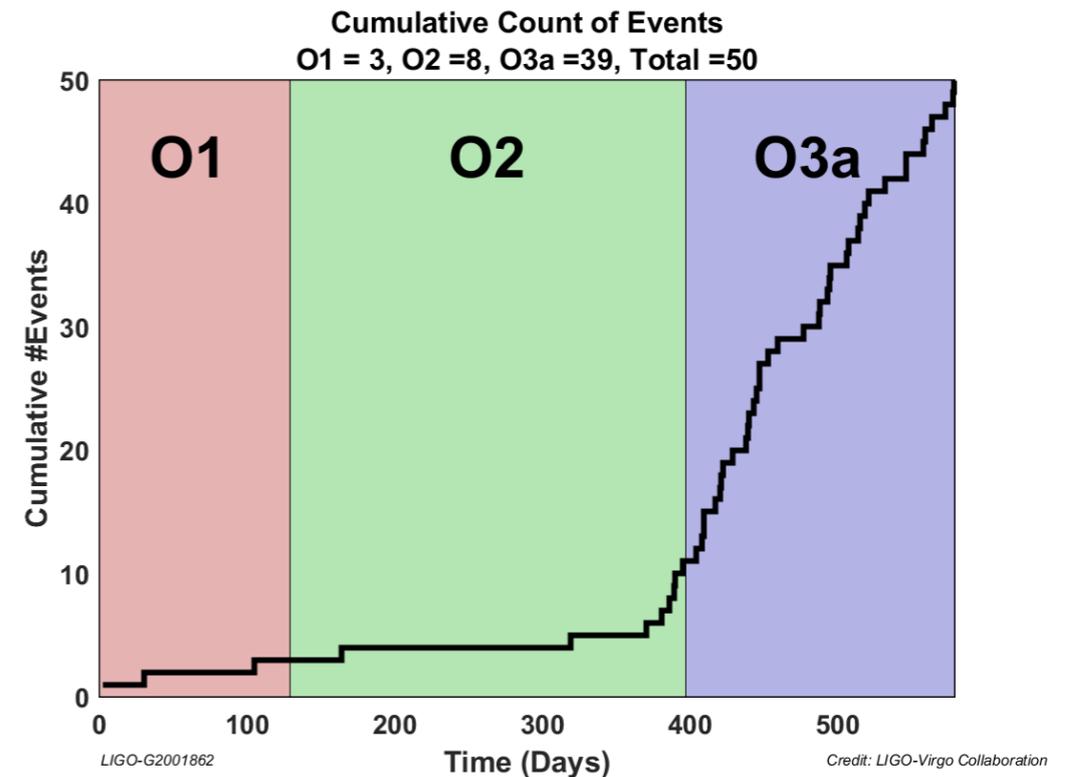
- Redshift: z
- Eccentricity: e (not discussed much because of circularization)



- $m_1 \gg m_2$
- $S_1 \neq 0$
- $S_2 = 0$

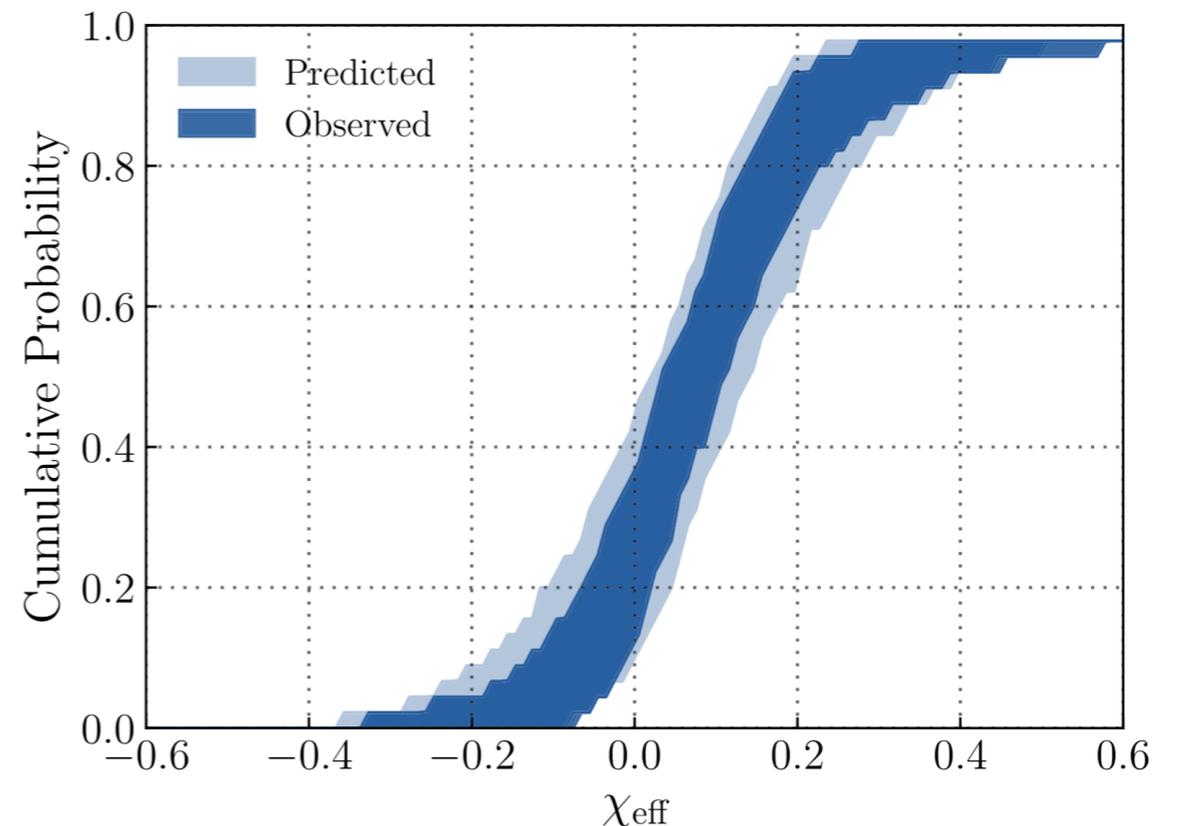
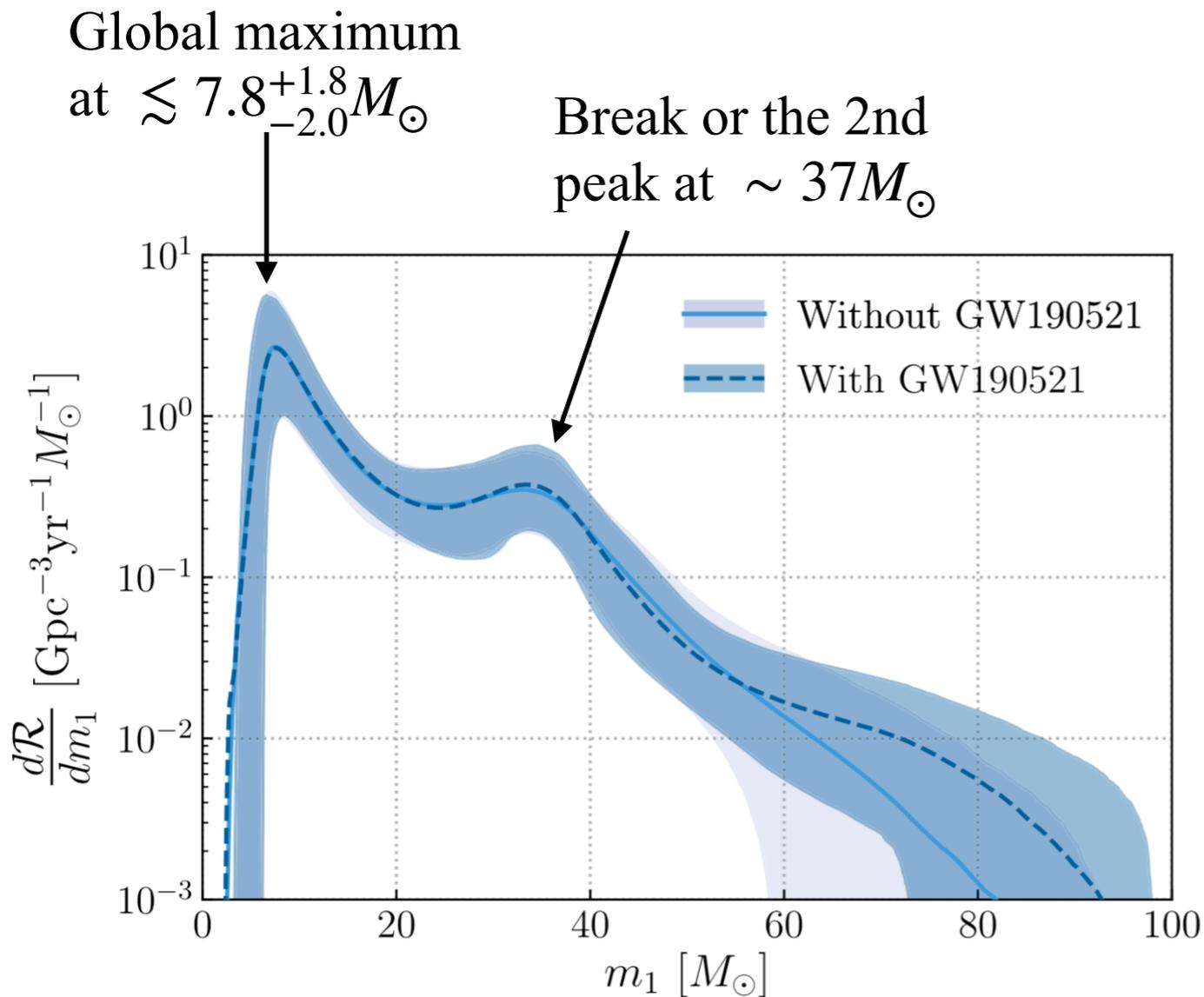
GW observing runs

- O1: 12 Sep. 2015 to 19 Jan. 2016
 - LIGO-Livingston (L)
 - LIGO-Hanford (H)
- O2: 30 Nov. 2016 to 25 Aug. 2017
 - Virgo (V) joined.
- O3a: 1 Apr. 2019 to 1 Oct. 2019
 - L: 88Mpc to 135Mpc for NS-NS
 - H: 66Mpc to 108Mpc
 - V: 26Mpc to 45Mpc
- O3b: 1 Nov. 2019 to 27 Mar. 2020
 - Not published



Properties of BH mergers

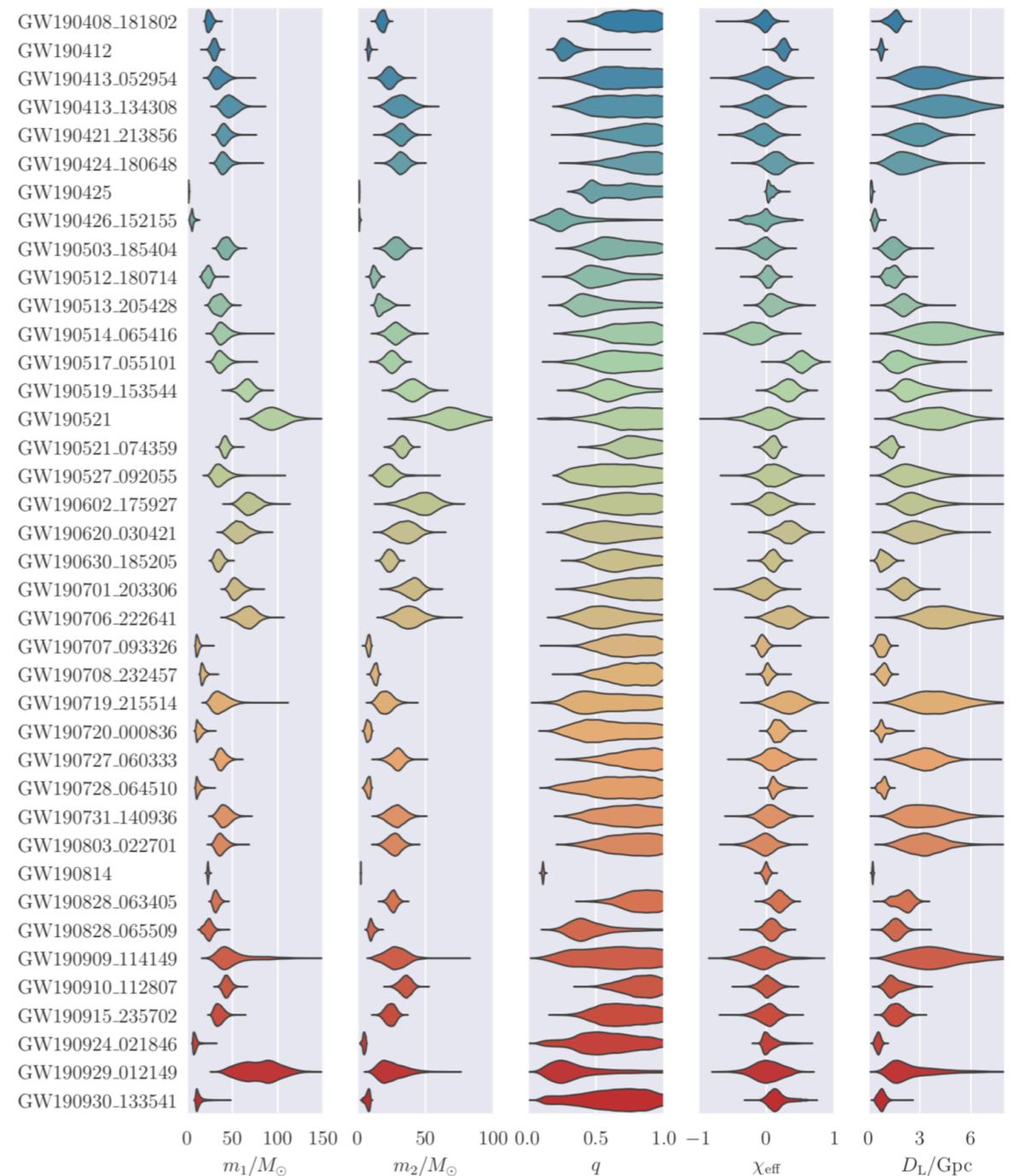
- The local BH merger rate density:
 $R \sim 23.9_{-8.6}^{+14.3} \text{ [yr}^{-1} \text{ Gpc}^{-3}\text{]}$



- Isolated binary: aligned spins
- Star cluster: isotropic spins
 \rightarrow Mixed with the two channels?
 (But see Bavera et al. 2020)

How about the errors

- Not small
- Mass seems to contain errors of a few 10 %.
 - But, it may not affect the mass distribution.
- Spin seems to be consistent with $\chi_{\text{eff}} = 0$ for all events.
 - We cannot assess if isolated binary evolution or star cluster are correct.
- At least, BH-BHs have not to have large χ_{eff} .



Abbott et al. (2020, arXiv:2010.14527)

Peculiar events

- GW190412

- $q \sim 0.25$ ($m_1 = 31.7_{-3.5}^{+3.6} M_{\odot}$, $m_2 = 8.0_{-0.7}^{+0.9} M_{\odot}$)

- Typical BH mergers: $q \sim 1$

- GW190814

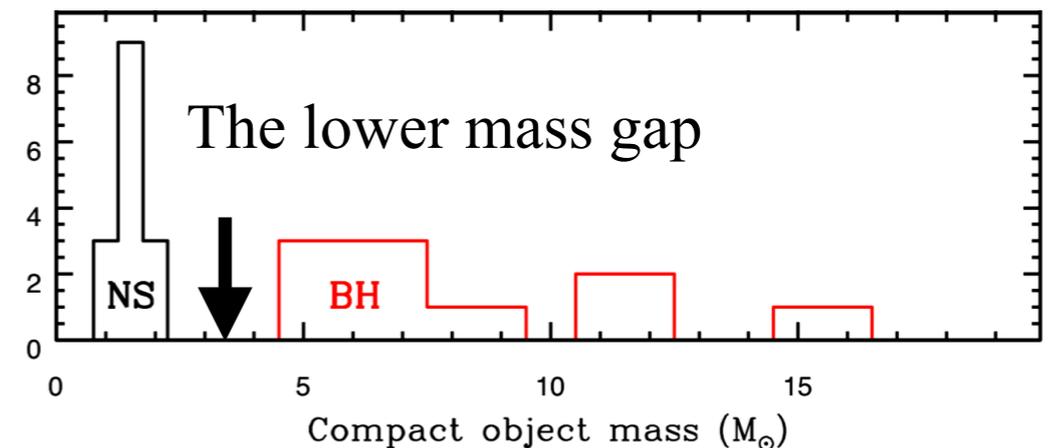
- $m_1 = 23.2_{-0.9}^{+1.0} M_{\odot}$

- $m_2 = 2.59_{-0.08}^{+0.08} M_{\odot}$

- BH-BH, BH-NS, or other?

- GW190521 (later)

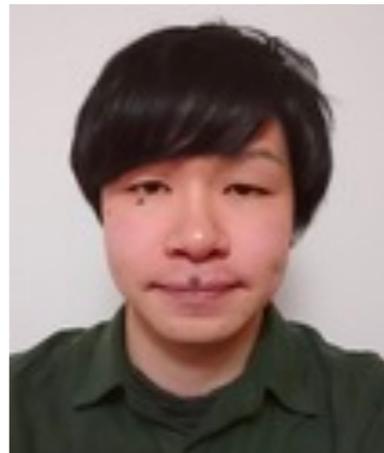
Casares et al. (2017)



Our study

- There is no confirmed formation scenario.
- More than one formation scenario may be correct.
- We make predictions of BH merger properties.
 - Open clusters
 - Pop III binary stars

Merging binary BHs formed in open clusters



Kumamoto J.



Trani A. A.

Open clusters

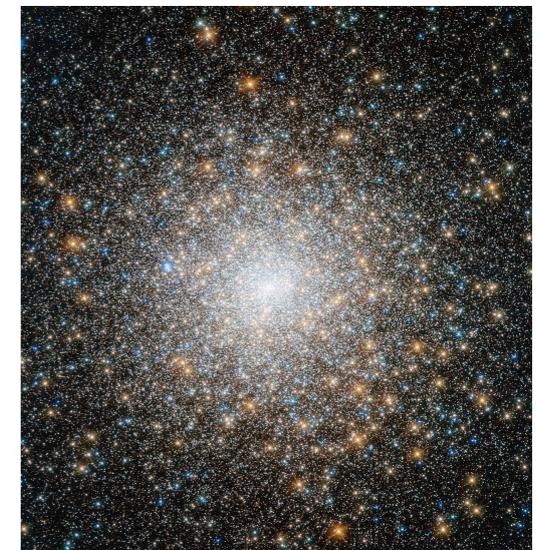
- Open clusters
 - $M_{\text{tot}} \sim 10^3 - 10^4 M_{\odot}$
 - $T_{\text{life}} \sim 100 \text{ Myr}$
- Globular cluster
 - $M_{\text{tot}} \sim 10^5 - 10^6 M_{\odot}$
 - $T_{\text{life}} \gtrsim 10 \text{ Gyr}$
- Why open clusters?
 - Forming currently
 - Many formed previously

***Promising formation sites
of merging binary BHs***

Open cluster (Pleiades)

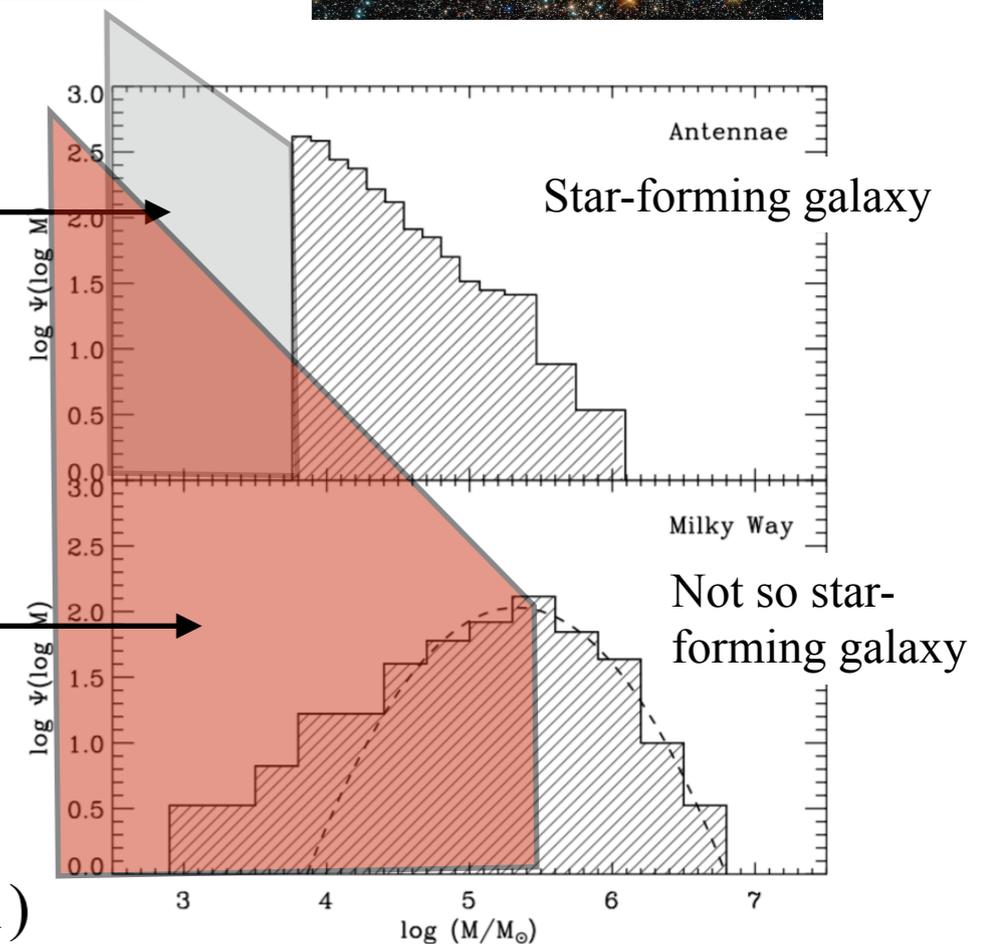


Globular cluster (M15)



Undetectable,
but present

Disrupted,
but formed



Fall, Zhang (2001)

Methods

- NBODY6++GPU code

- N-body simulation

$$\frac{d^2\vec{r}_i}{dt^2} = \sum_j^N \frac{Gm_j}{|\vec{r}_j - \vec{r}_i|^3} (\vec{r}_j - \vec{r}_i)$$

- Single star evolution

- **Main sequence** → **Giant** (→ **Helium star**) → **BH**
(Hurley et al. 2000)

- Stellar wind mass loss (Belczynski et al. 2010)

- Supernova model (Belczynski et al. 2002)

- Binary star evolution (Hurley et al. 2002)

- Tidal interaction, **common envelope**, stable mass transfer, magnetic braking, etc.

- Initial conditions

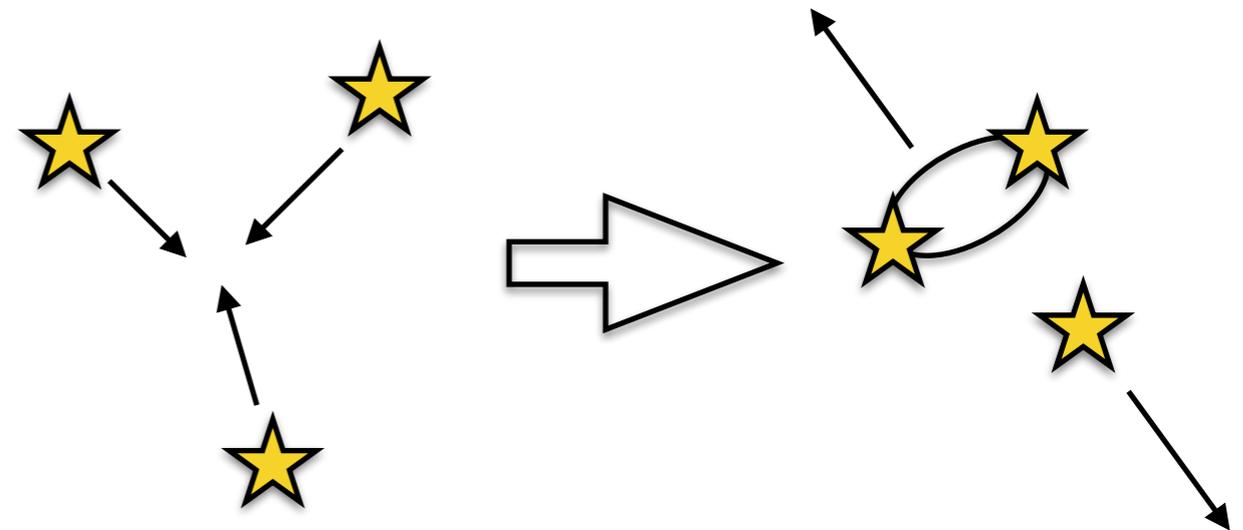
- $M_{\text{cl,tot}} \sim 2500M_{\odot}$, $\rho_{\text{hm}} \sim 10^4 M_{\odot} \text{pc}^{-3}$

- Kroupa's IMF ($0.08M_{\odot} < m_* < 150M_{\odot}$)

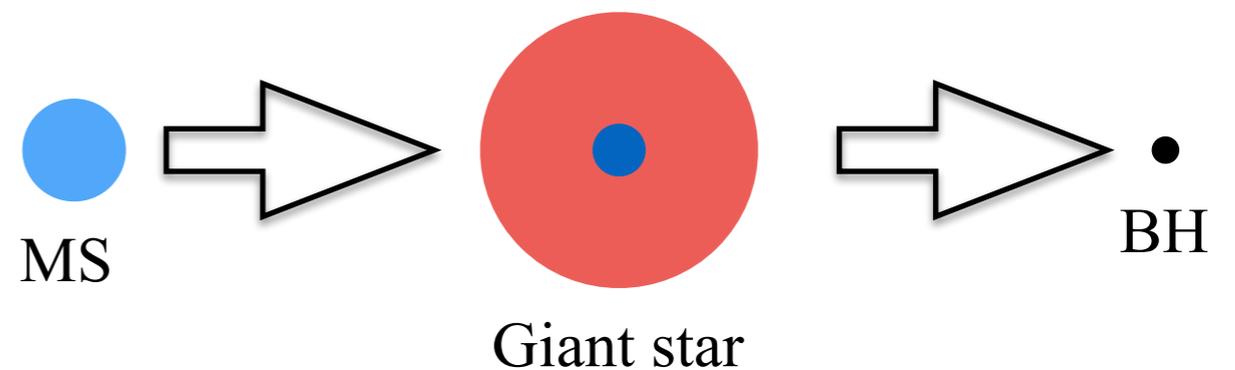
- $Z = 0.1, 0.25, 0.5, 1Z_{\odot}$

- Several 100 clusters for each metallicity

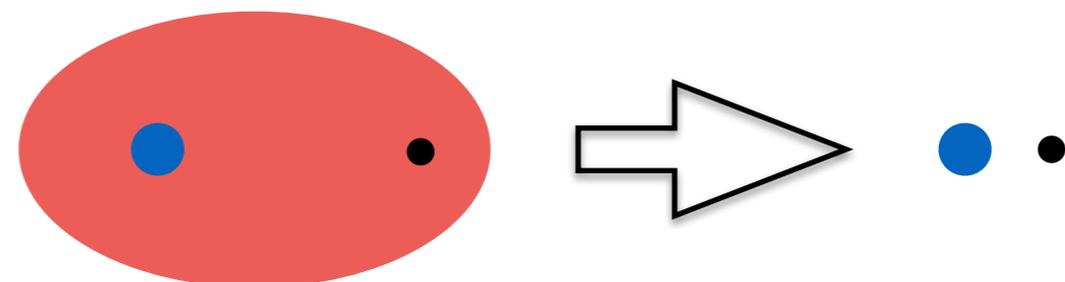
Dynamical binary formation



Single star evolution

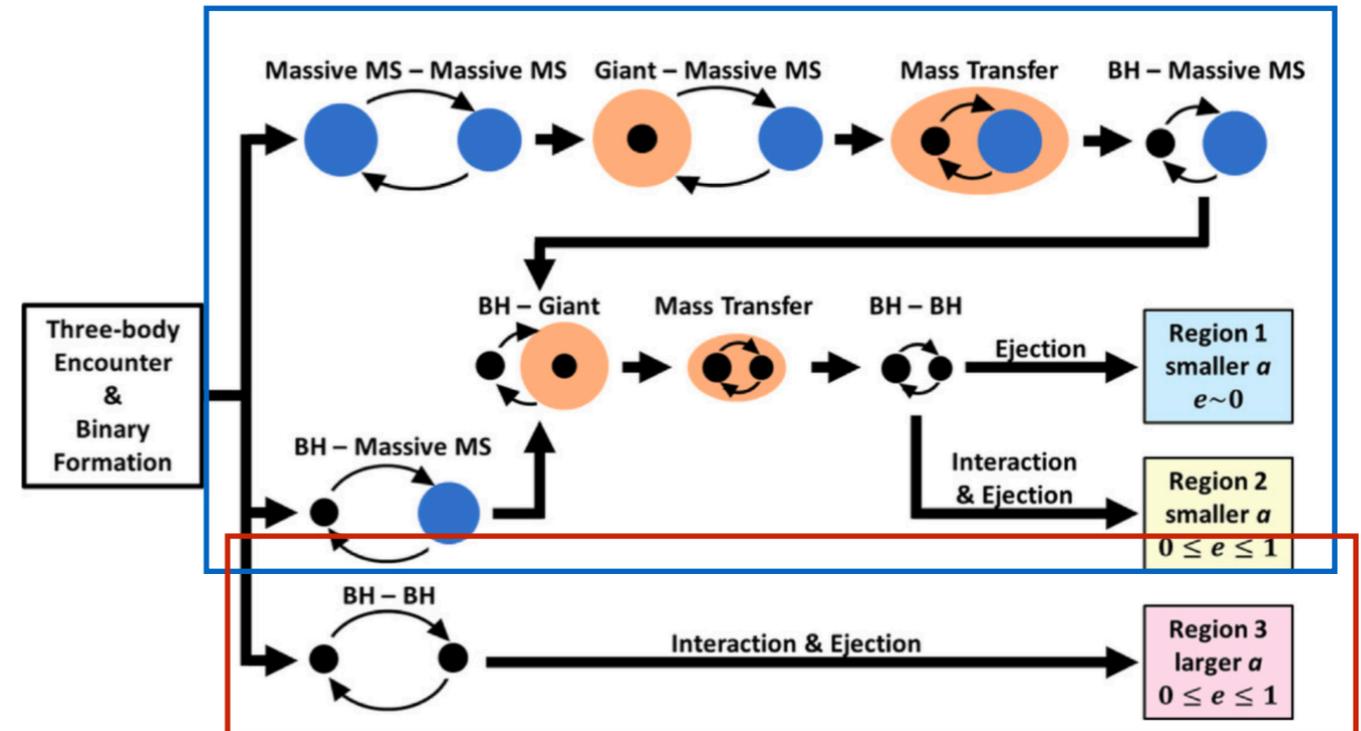


Binary star evolution (common envelope)



Formation channels

- High metallicity ($Z = Z_{\odot}$)
 - Dynamical formation of merging binary BHs
 - Similar to globular clusters
- Low metallicity ($Z < Z_{\odot}$)
 - Dynamical formation of main-sequence binary, and orbital shrink through common envelope
 - Similar to isolated binary evolution
- Clue to identify BH-BH origin?

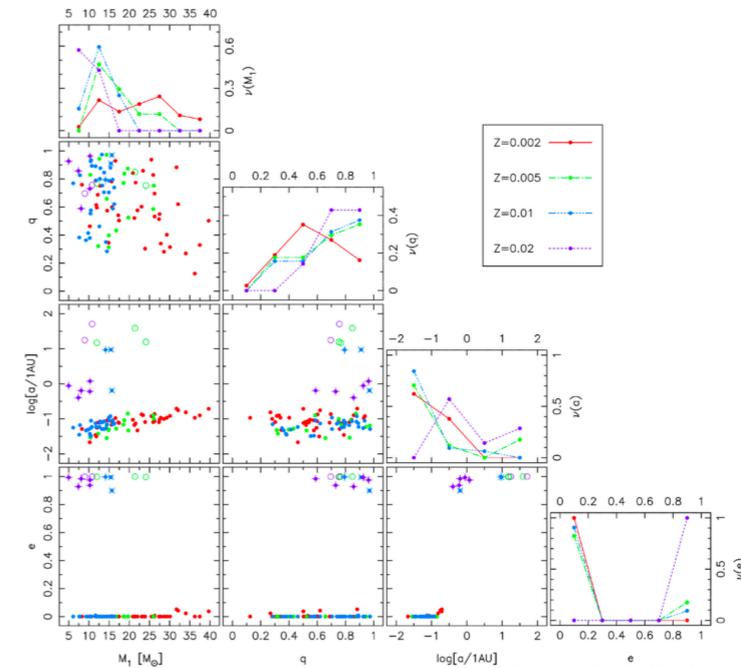


Kumamoto et al. (2019)

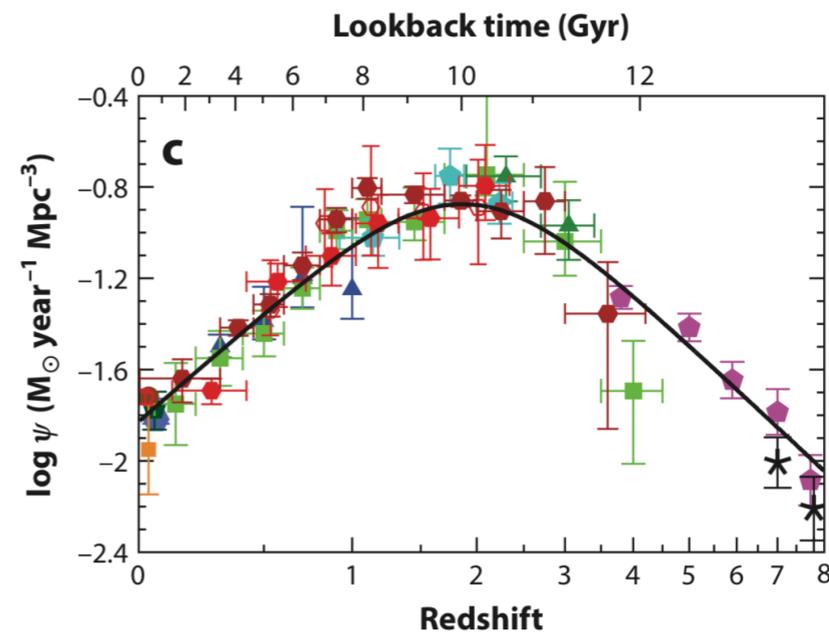
- Dynamical formation of BHs
 - $Z = Z_{\odot}$: binary BHs compact, because of low mass ($\lesssim 10M_{\odot}$)
 - $Z < Z_{\odot}$: binary BHs not compact, because of high mass ($\gtrsim 10M_{\odot}$)
- Common envelope
 - $Z = Z_{\odot}$: no envelope because of strong stellar wind
 - $Z < Z_{\odot}$: sufficient envelope because of weak stellar wind

Estimate of BH merger rate

- N-body results
 - The number of merging binary BHs
 - m_1, m_2, a, e
- Star formation history
 - Total star formation rate (Madau, Fragos 2017)
 - Cosmic evolution of metallicity distribution (Chruslinska, Nelemans 2019)
 - Cluster mass fraction: 20%



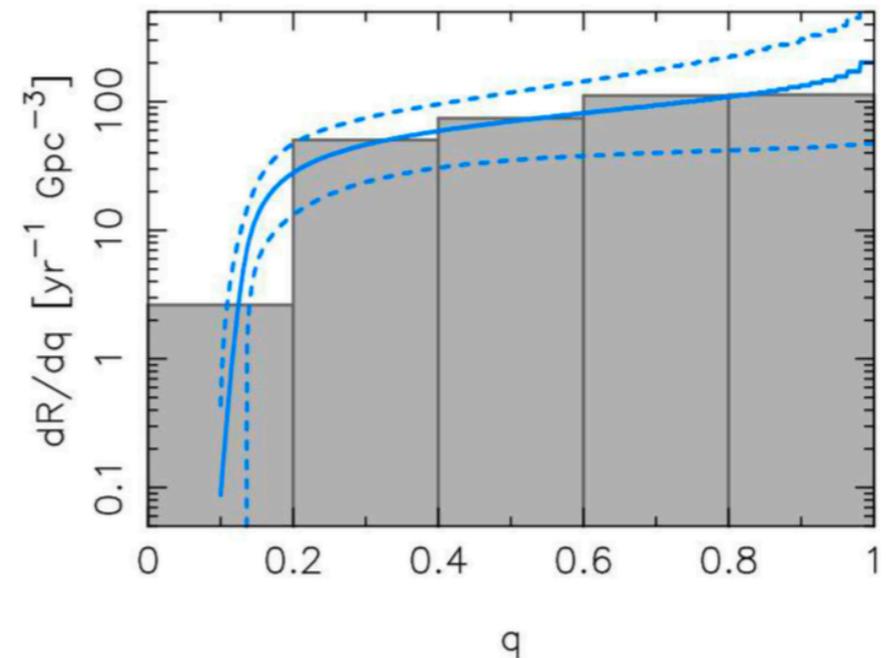
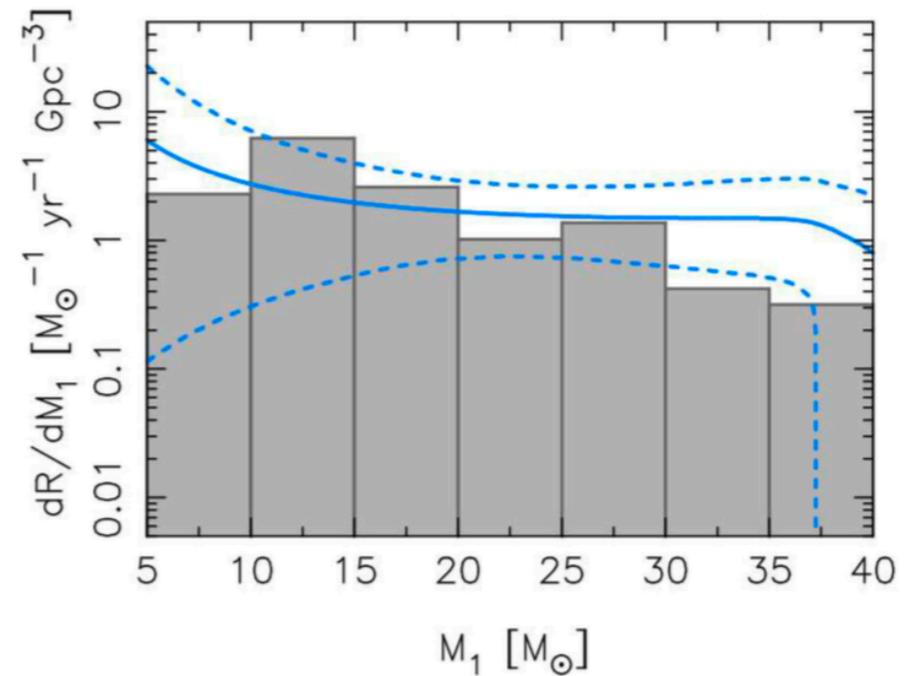
Kumamoto et al. (2020)



Madau, Dickinson (2014)

Mass distribution

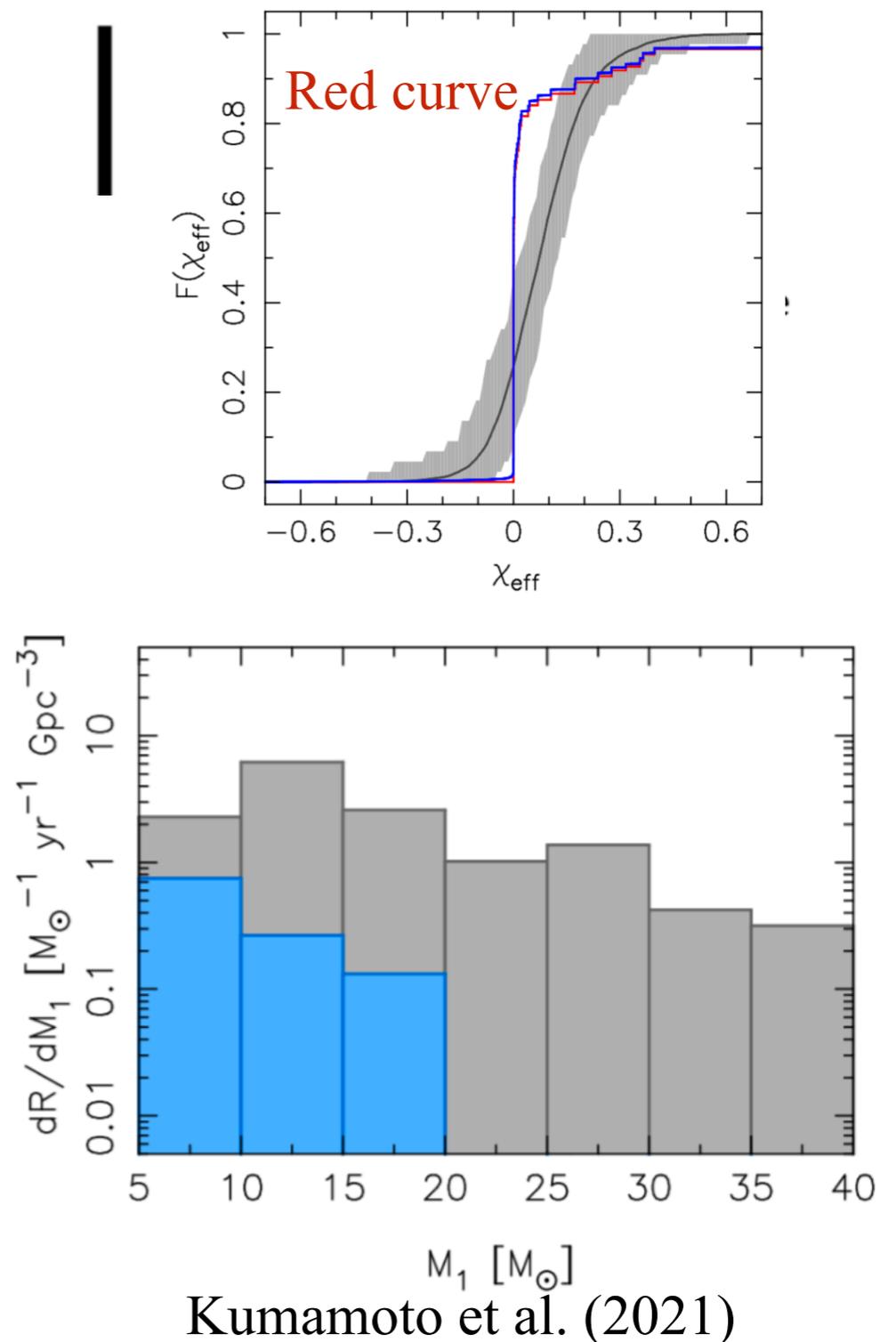
- $R \sim 70 \text{ yr}^{-1} \text{ Gpc}^{-3}$
- Consistent with GW observations, at least for $\lesssim 40M_{\odot}$
- Require $Z < 0.1Z_{\odot}$ open clusters, and more sophisticated initial conditions for $\gtrsim 40M_{\odot}$



Kumamoto et al. (2020)

Spin distribution

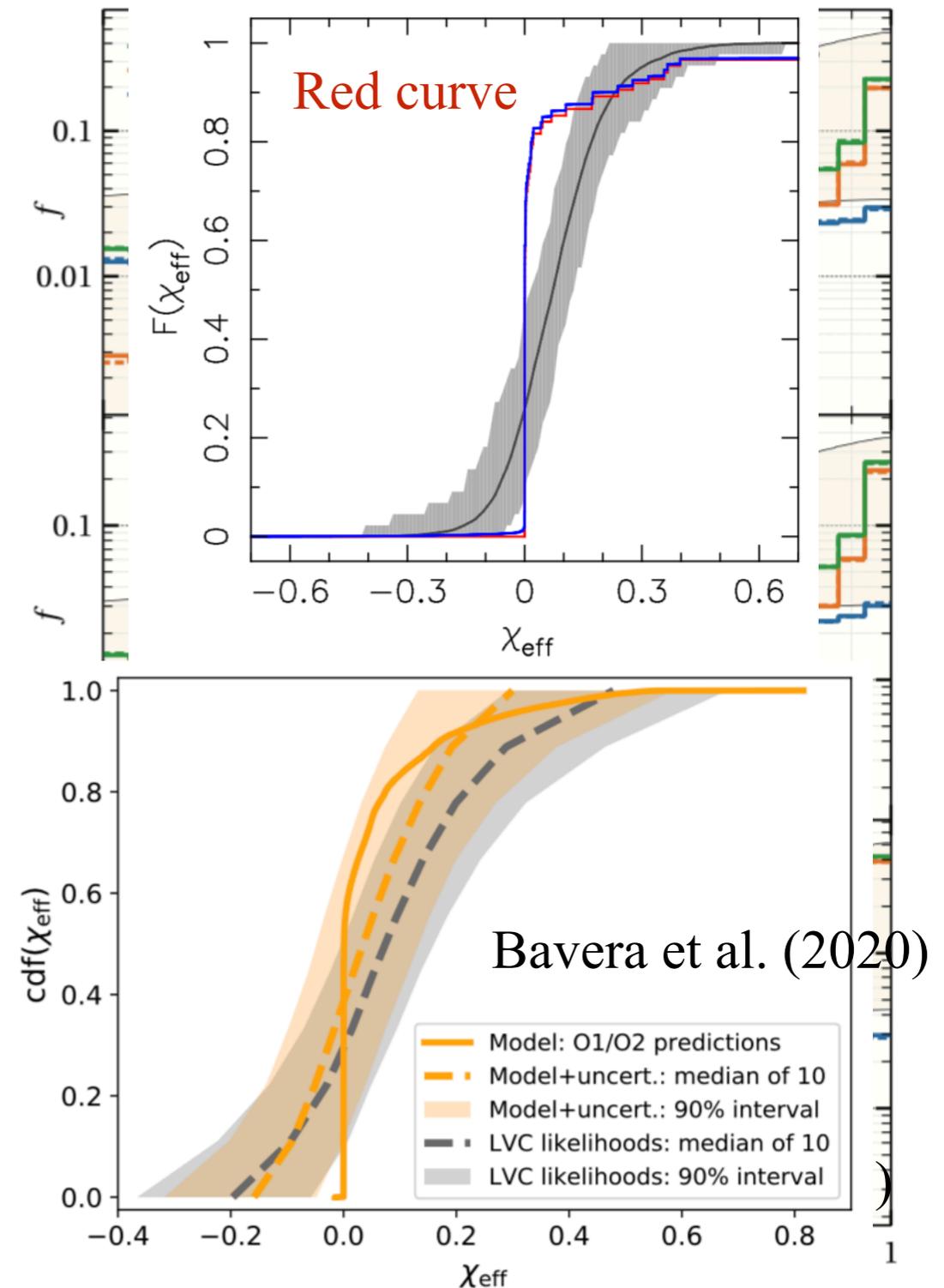
- Spin generated through tidal interactions during BH progenitors (Kushnir et al. 2016; Hotokezaka, Piran 2017)
- 90% zero spin, 10% non-negligible spin, 0% negative spin
- Negative correlation between mass and spin



Spin misalignment

- 10 % of merging BHs can interact with another BH before they merge.
- Their spins can be misaligned through single close encounter in open clusters.
- Negative spin, but small fraction

Trani et al. (2021, MNRAS, 504, 910)



Pair instability mass gap
event: GW190521

GW190521

- Merger of $85^{+21}_{-14} M_{\odot}$ and $66^{+17}_{-18} M_{\odot}$ BHs
- The primary BH has only a 0.32% probability of being below $65 M_{\odot}$.
- Pair instability mass gap: $40 - 130 M_{\odot}$
- Possible scenarios
 - Cluster origins (Rodriguez et al. 2019; Di Carlo et al. 2020; Tagawa et al. 2020; Fragione et al. 2020; Rizzuto et al. 2021)
 - Uncertainty of PI mass gap boundary (Farmer et al. 2020; Belczynski et al. 2020; Costa et al. 2021)
 - **Uncertainty of convective overshoot**

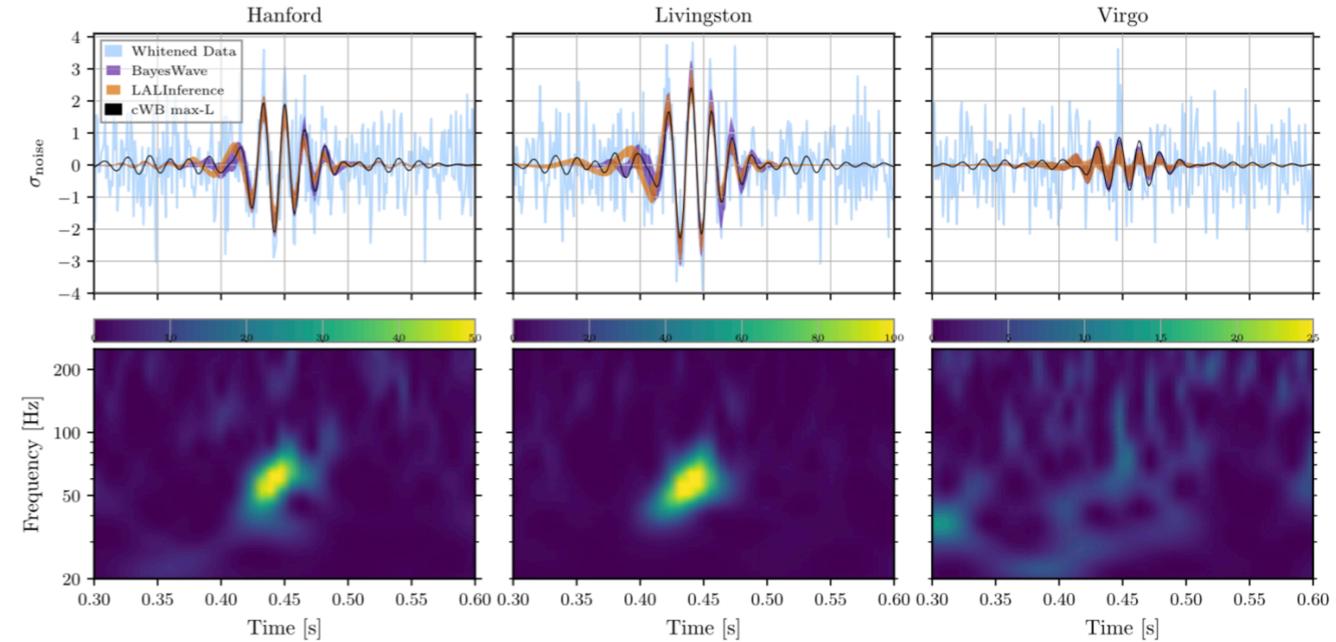
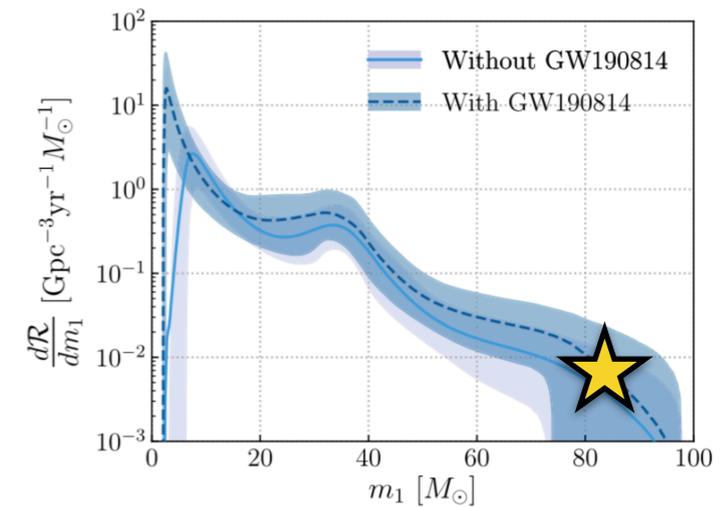


TABLE I. Parameters of GW190521 according to the NRSur7dq4 waveform model. We quote median values with 90% credible intervals that include statistical errors.

| Parameter | |
|---|-----------------------------|
| Primary mass | $85^{+21}_{-14} M_{\odot}$ |
| Secondary mass | $66^{+17}_{-18} M_{\odot}$ |
| Primary spin magnitude | $0.69^{+0.27}_{-0.62}$ |
| Secondary spin magnitude | $0.73^{+0.24}_{-0.64}$ |
| Total mass | $150^{+29}_{-17} M_{\odot}$ |
| Mass ratio ($m_2/m_1 \leq 1$) | $0.79^{+0.19}_{-0.29}$ |
| Effective inspiral spin parameter (χ_{eff}) | $0.08^{+0.27}_{-0.36}$ |
| Effective precession spin parameter (χ_p) | $0.68^{+0.25}_{-0.37}$ |
| Luminosity Distance | $5.3^{+2.4}_{-2.6}$ Gpc |
| Redshift | $0.82^{+0.28}_{-0.34}$ |
| Final mass | $142^{+28}_{-16} M_{\odot}$ |
| Final spin | $0.72^{+0.09}_{-0.12}$ |
| P ($m_1 < 65 M_{\odot}$) | 0.32% |
| \log_{10} Bayes factor for orbital precession | $1.06^{+0.06}_{-0.06}$ |
| \log_{10} Bayes factor for nonzero spins | $0.92^{+0.06}_{-0.06}$ |
| \log_{10} Bayes factor for higher harmonics | $-0.38^{+0.06}_{-0.06}$ |

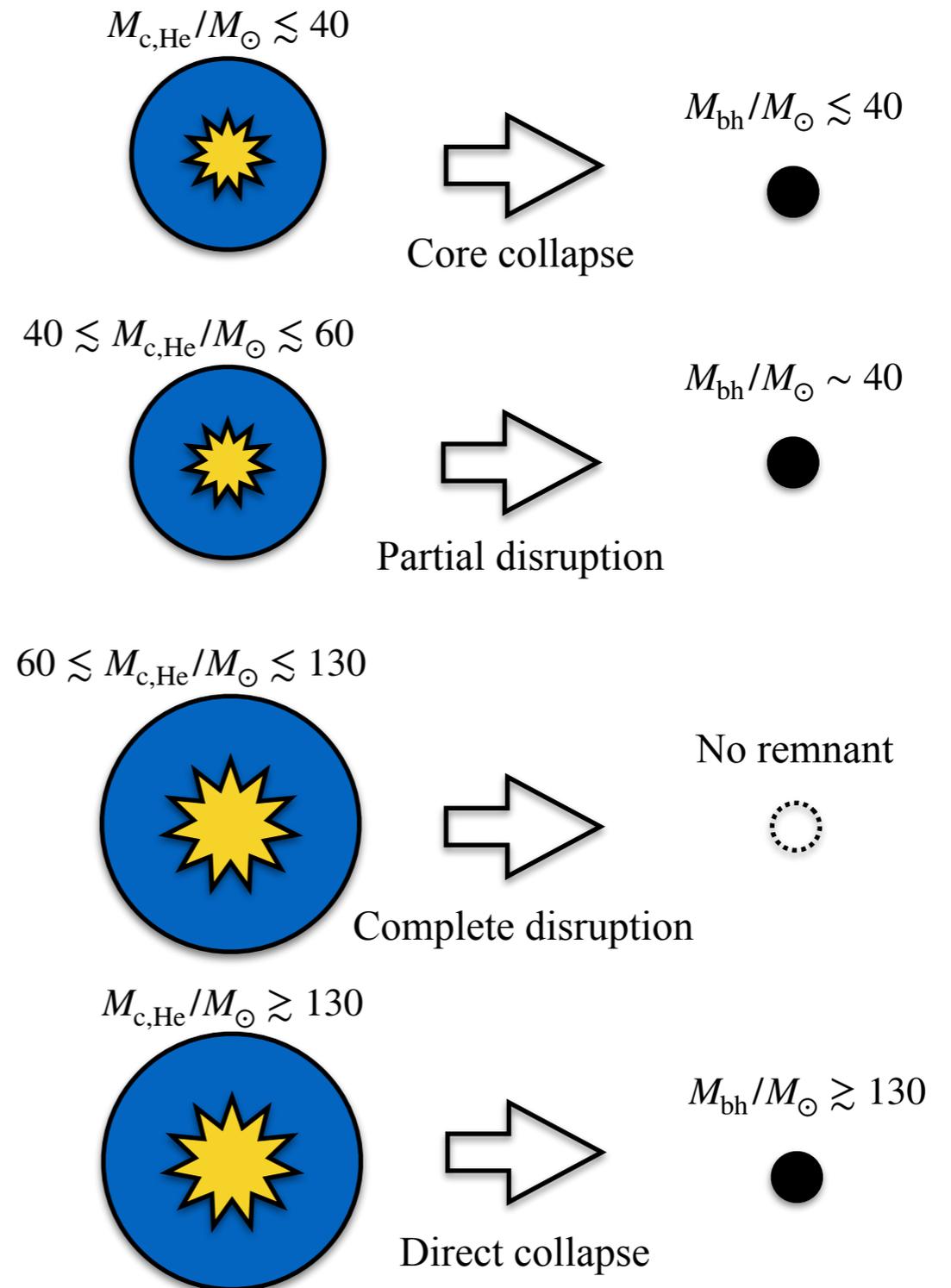


Abbott et al. (2021)

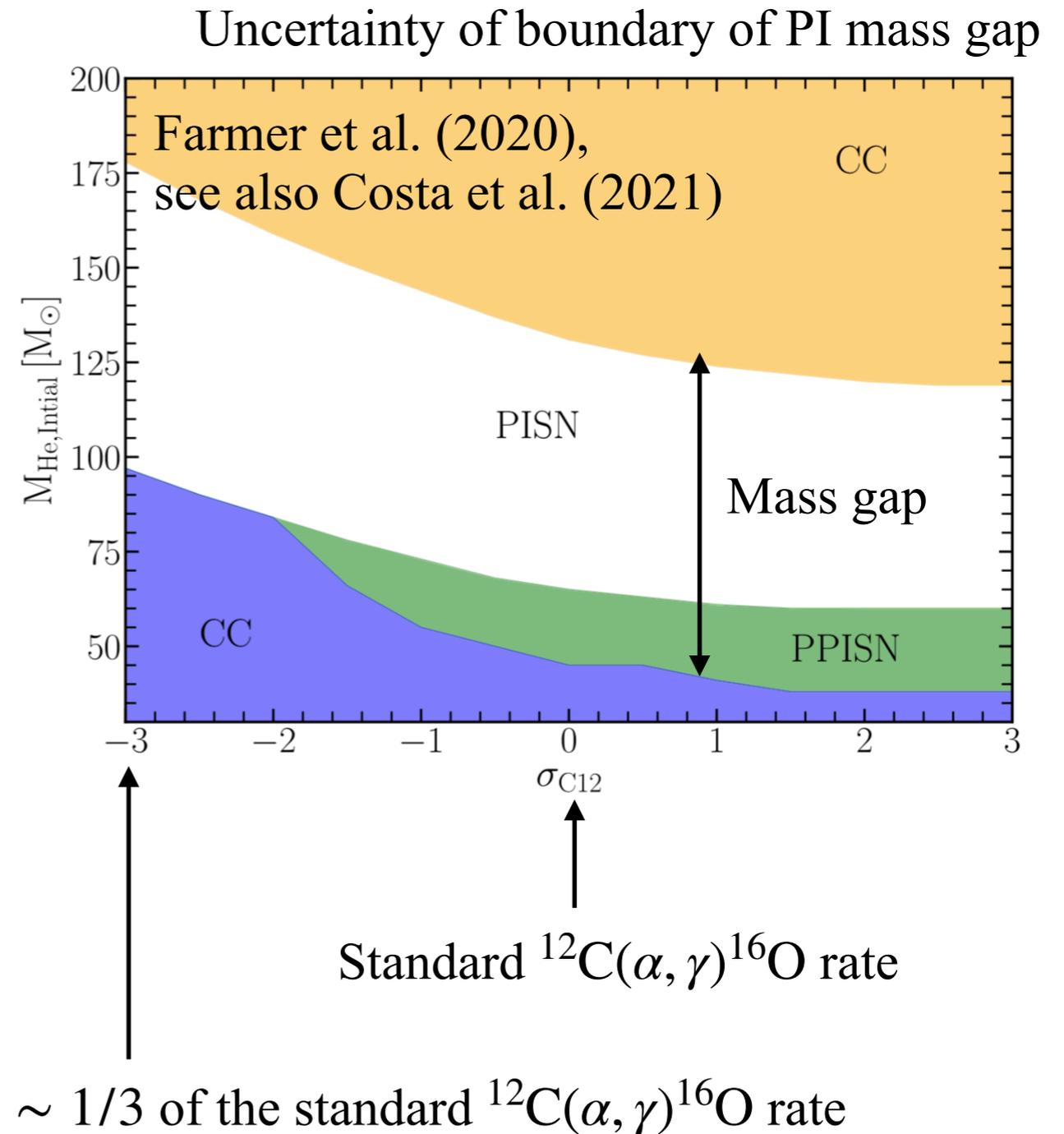
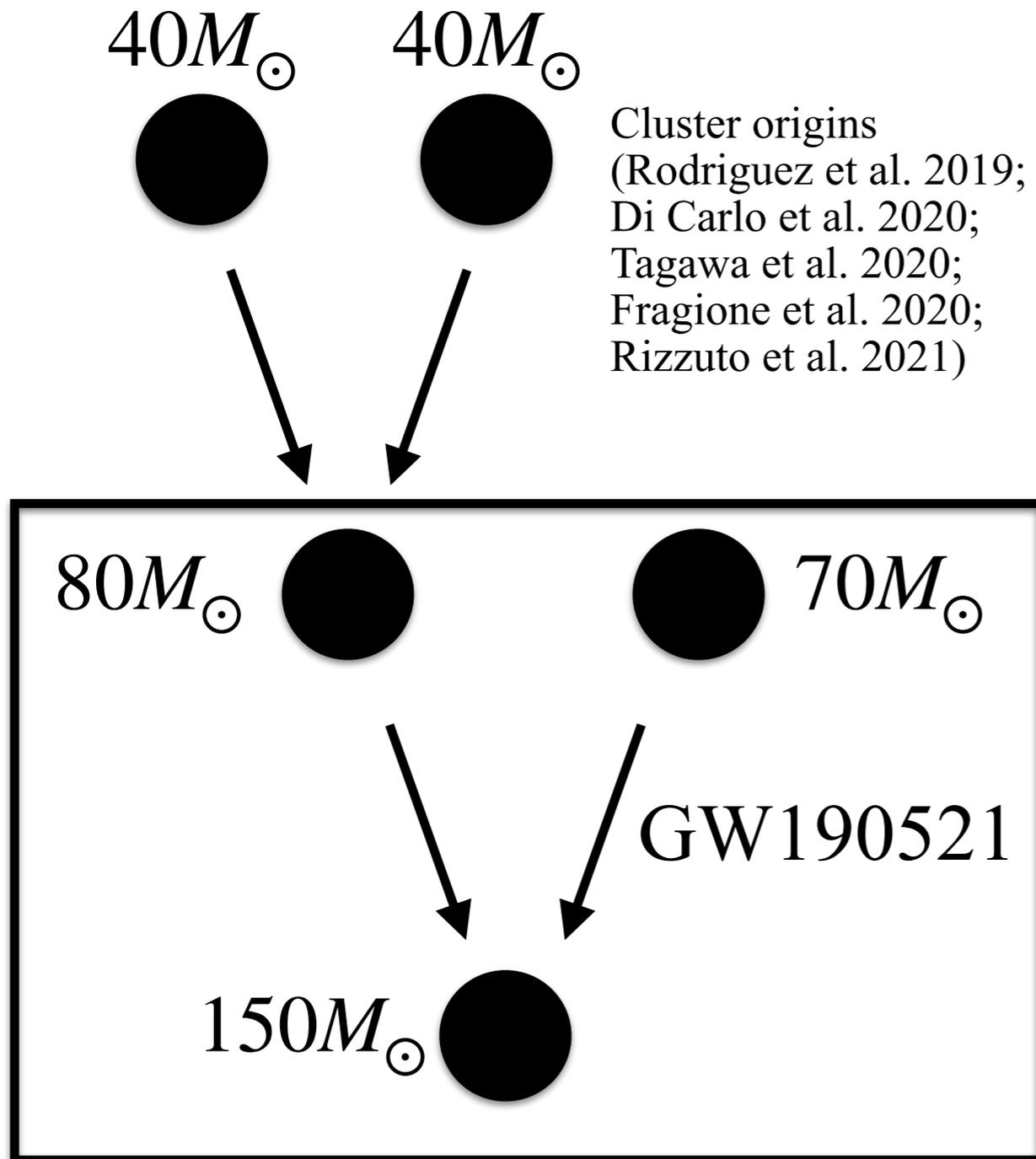
Abbott et al. (2020)

Pair instability (PI) mass gap

- Pair instability
 - Gamma-ray absorption in creating electron-positron pairs
 - Stellar contraction
 - Runaway nuclear reaction
 - Stellar explosion
- Mass gap
 - Mass range without BHs
 - $40 - 130M_{\odot}$ by PI



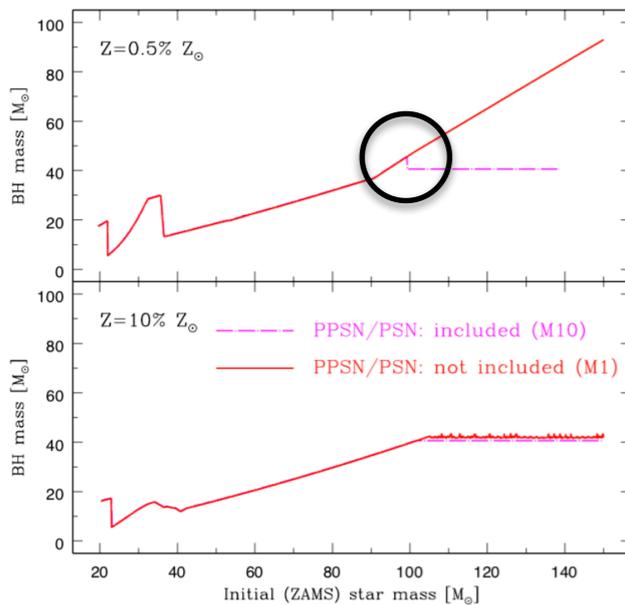
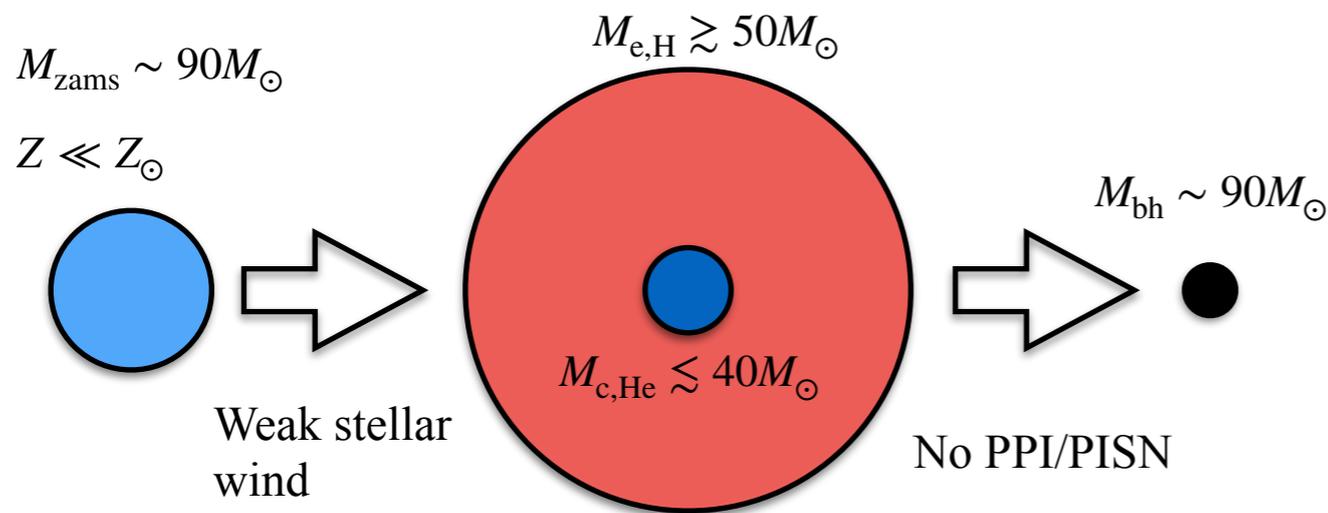
Many scenarios



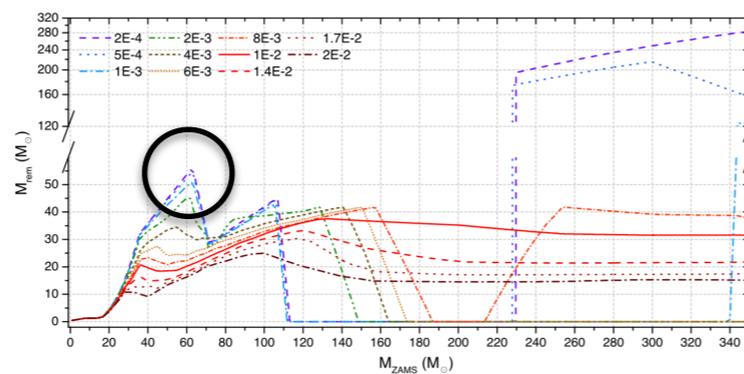
$\rightarrow 90M_{\odot}$ BH can be formed, avoiding PI.

Revisit of the PI mass gap

Single star evolution



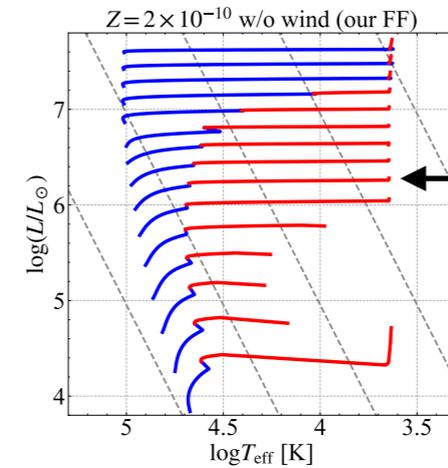
Belczynski et al. (2016)



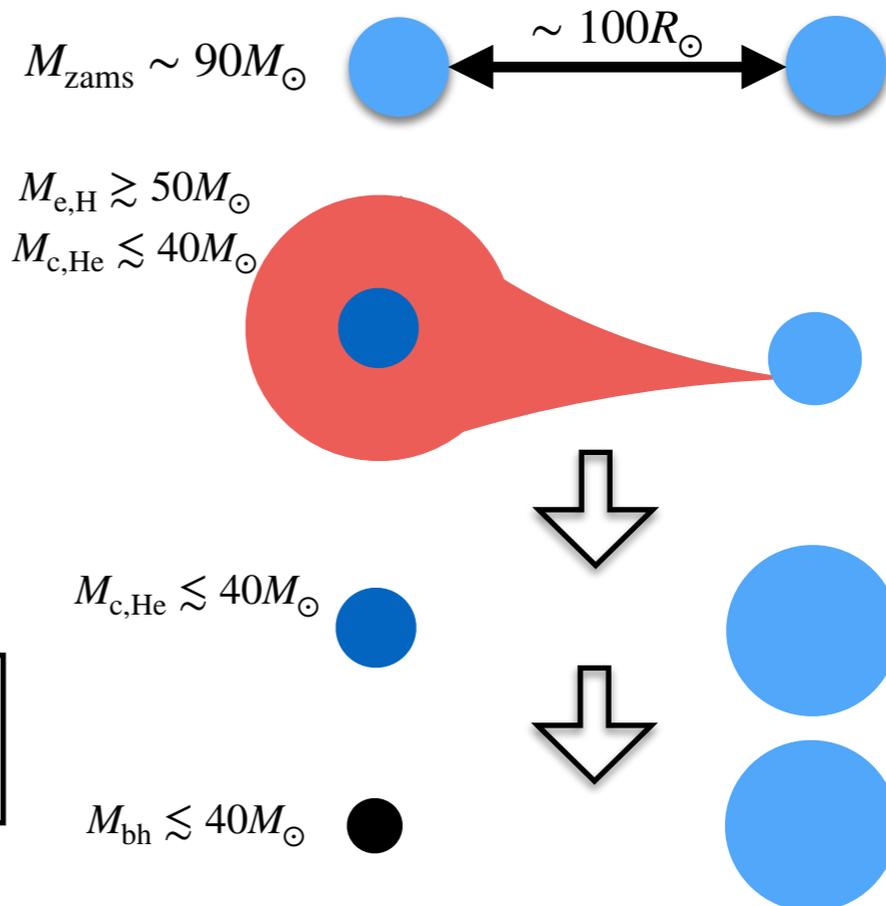
Spera, Mapelli (2017)

Single star can form PI mass gap BH *if it has massive envelope.*

Binary star evolution

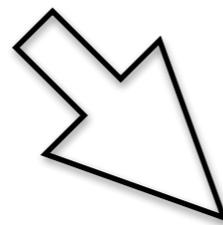
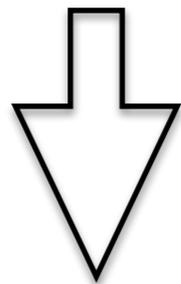
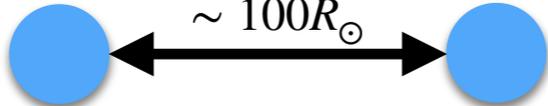


- $M_{\text{tot}} \sim 80M_{\odot}$
- $M_{\text{c}} \sim 40M_{\odot}$
- $R \gtrsim 10^3 R_{\odot}$



Stellar radius

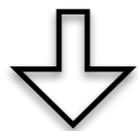
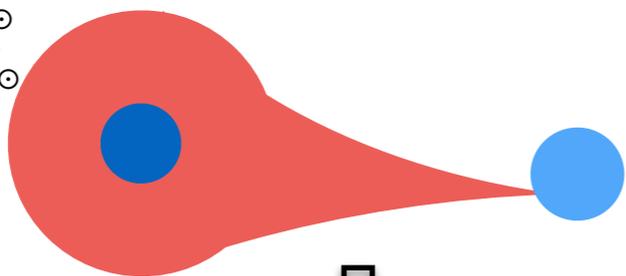
$M_{\text{zams}} \sim 90M_{\odot}$



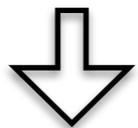
*Can a star keep its
radius $\lesssim 100R_{\odot}$?*

$M_{\text{e,H}} \gtrsim 50M_{\odot}$
 $M_{\text{c,He}} \lesssim 40M_{\odot}$

$R \gtrsim 1000R_{\odot}$



$M_{\text{c,He}} \lesssim 40M_{\odot}$

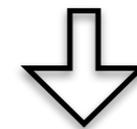
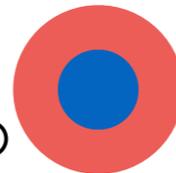


$M_{\text{bh}} \lesssim 40M_{\odot}$



$M_{\text{e,H}} \gtrsim 50M_{\odot}$
 $M_{\text{c,He}} \lesssim 40M_{\odot}$

$R \lesssim 100R_{\odot}$

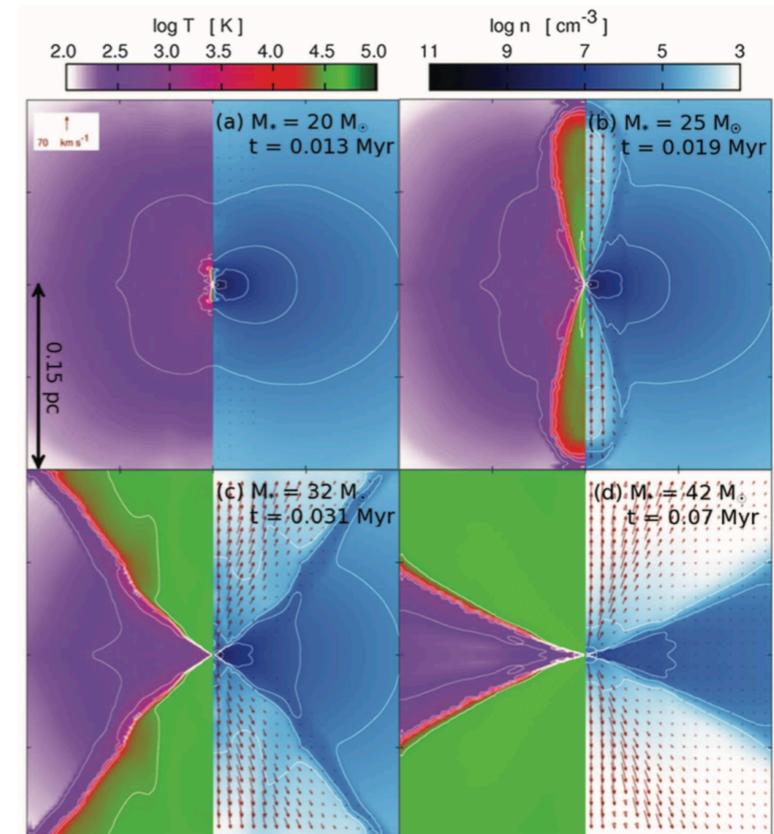
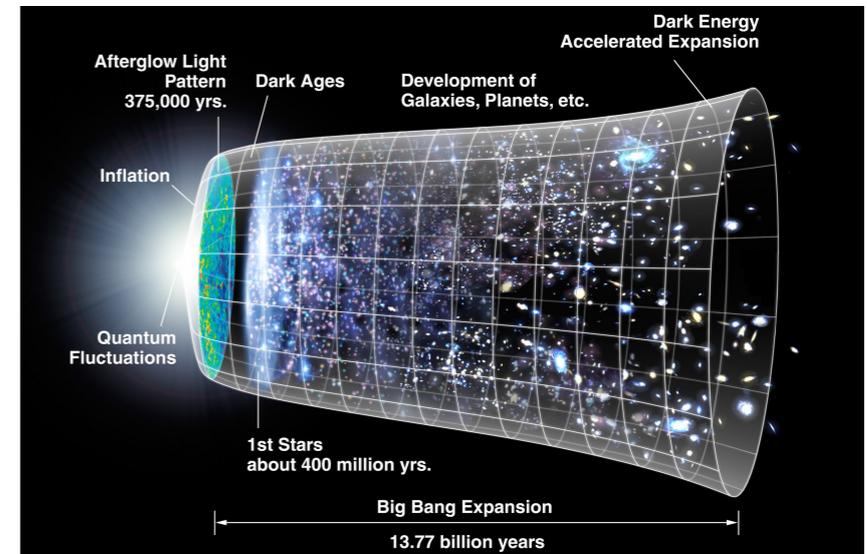


$M_{\text{bh}} \lesssim 40M_{\odot}$



Population III stars

- Consisting of primordial gas (mostly H and He)
- Born in the high-redshift universe
- Astrophysical importance: stellar nucleosynthesis, reionization, ...
- Top-heavy initial mass function (IMF) predicted theoretically (Omukai, Nishi 1998; Abel et al. 2002; Bromm, & Larson 2004)
- Not yet discovered (Frebel, Norris 2015 for review)

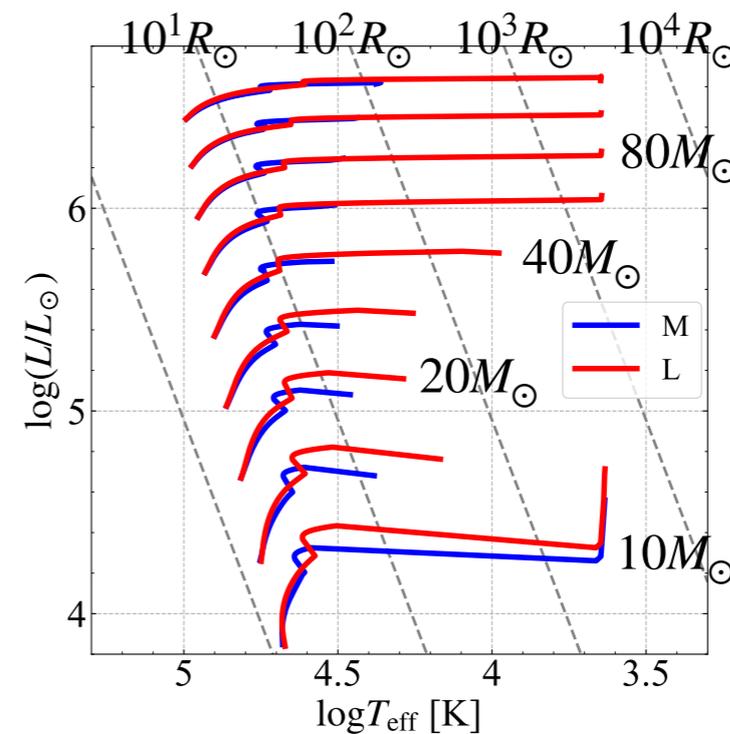
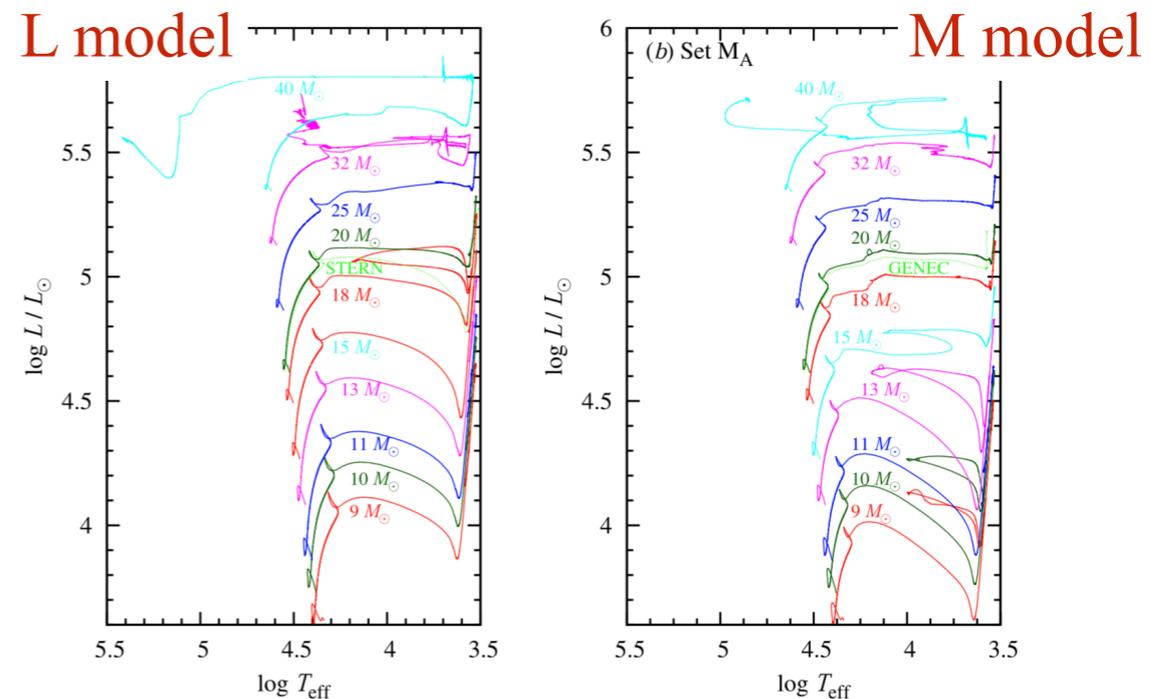


Hosokawa et al. (2011)

Pop III star evolution model

- No massive Pop. III stars discovered so far
- Extrapolation from nearby stars to Pop. III stars
 - L model: similar to Stern (Brott et al. 2011)
 - M model: similar to GENEC (Ekstrom et al. 2012; Farrell et al. 2020)
- The maximums radius of a $80M_{\odot}$ star
 - M model: $\sim 40R_{\odot}$, similar to Farrell et al. (2020)
 - L model: $\sim 3 \times 10^3 R_{\odot}$, similar to Yoon et al. (2012)

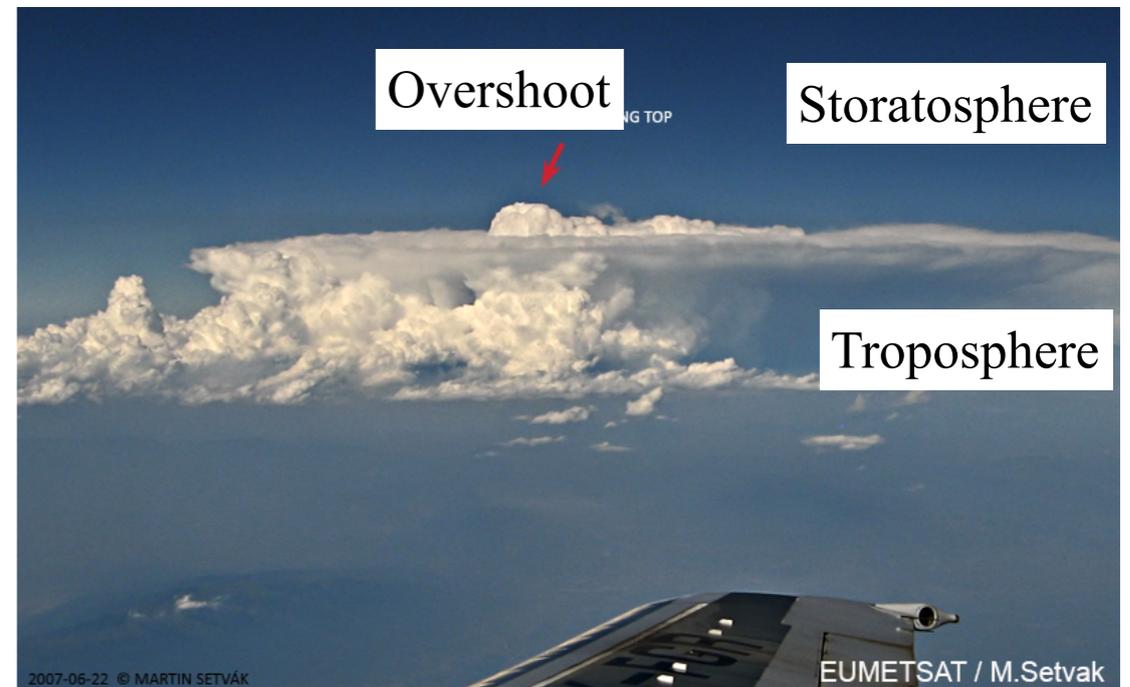
Yoshida et al. (2019)



Two Pop. III models

Convective overshoot

- More effective overshoot
 - Larger He core at the end of MS
 - Larger luminosity in post-MS
 - Larger radius in post-MS

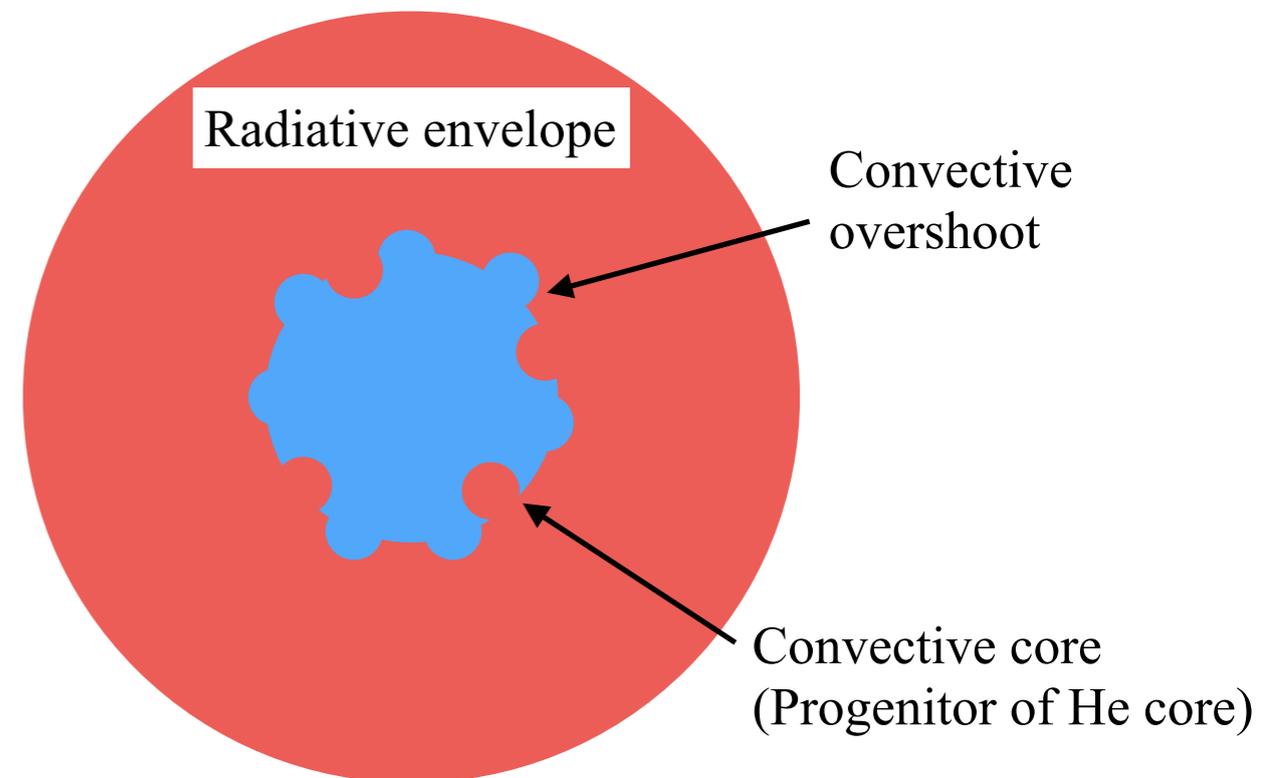


- Effectiveness of overshoot

- M model: less effective overshoot
- L model: more effective overshoot

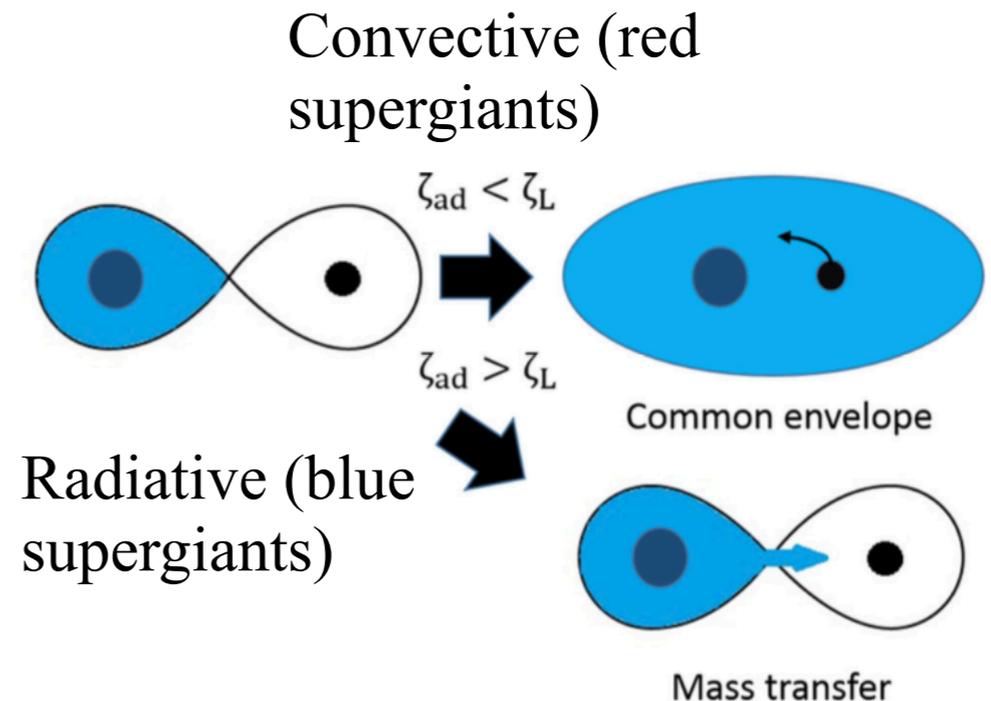
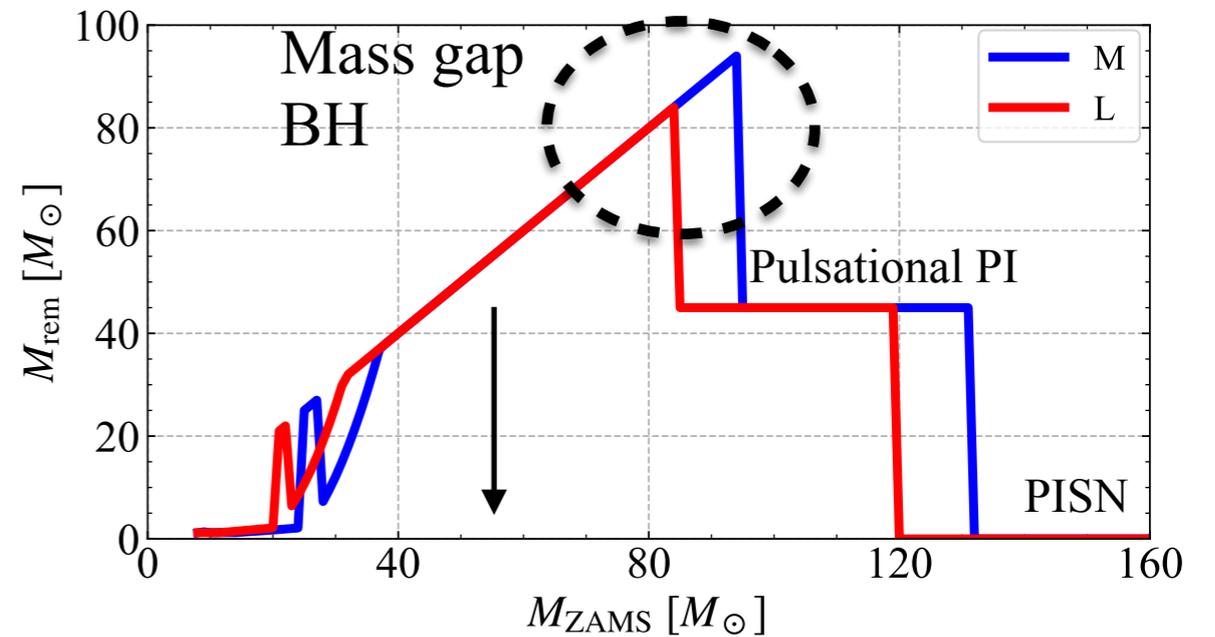
Both consistent
with Pop I/II stars

Different radii for
Pop III stars



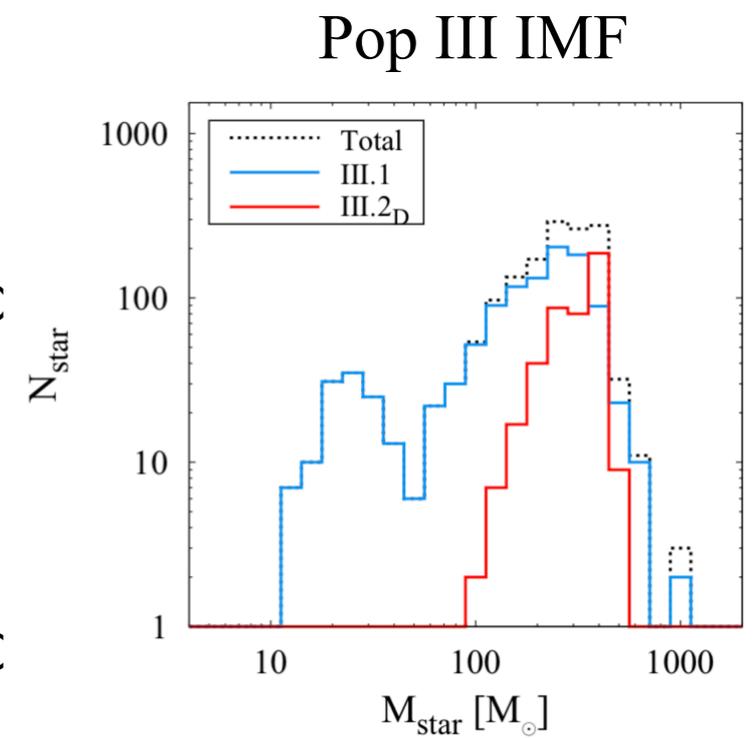
Numerical setup

- The L and M models
- No stellar wind
- Fryer's rapid model for supernova with pair instability (PI) model like the strong PI of Belczynski et al. (2020).
- No natal kick
- Stellar envelope property in Post-MS phases
 - Radiative: $\log(T_{\text{eff}}) > 3.65$
 - CHeB phase in the original BSE
 - Convective: $\log(T_{\text{eff}}) < 3.65$
 - AGB phase in the original BSE



Initial conditions

- Instantaneous formation of Pop III stars: $\sim 10^{13} M_{\odot} \text{Gpc}^{-3}$ at $z \sim 10$
 - Consistent with numerically predicted results (Magg et al. 2016; Skinner, Wise 2020; but see Inayoshi et al. 2021)
- Binary fraction: 1 (e.g. Sugimura et al. 2020)
- Primary IMF: $f(m_1) \propto m_1^{-1}$ ($10M_{\odot} \leq m_1 \leq 150M_{\odot}$)
- Mass ratio: $f(q) \propto \text{const}$ ($10M_{\odot}/m_1 \leq q \leq 1$)
- Semi-major axis: $f(a) \propto a^{-1}$ ($10R_{\odot} \leq a \leq 2000R_{\odot}$)
- Eccentricity: $f(e) \propto e$

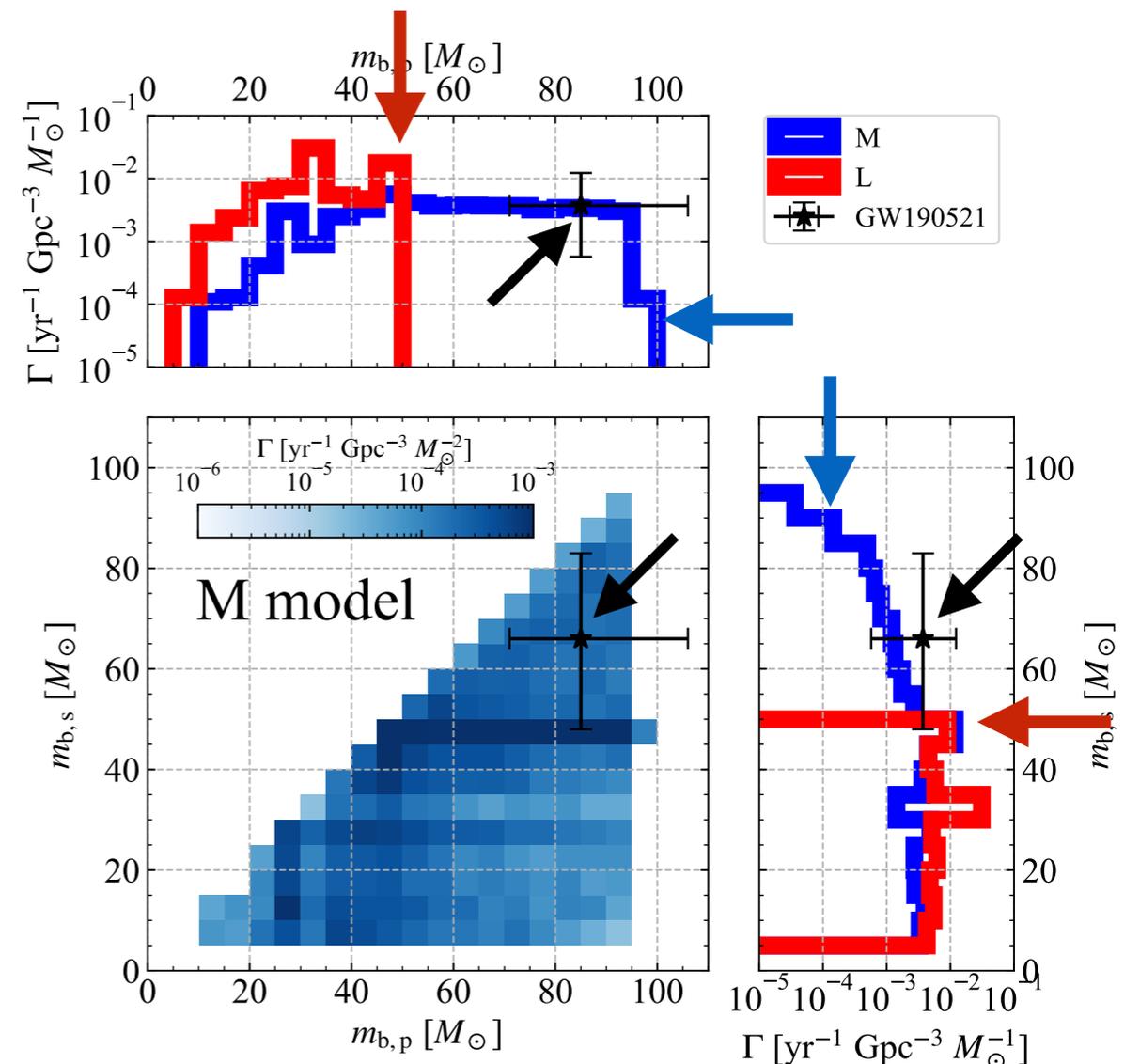


Hirano et al. (2015)

BH mass distribution

- M model
 - The maximum mass: $\sim 100M_{\odot}$
 - Stars lose little mass through binary interactions.
 - Pop. III stars can form GW190521-like BH-BHs.
- L model
 - The maximum mass: $\sim 50M_{\odot}$
 - Stars lose their H envelopes through binary interactions
 - No Pop. III stars can form GW190521-like BH-BHs.

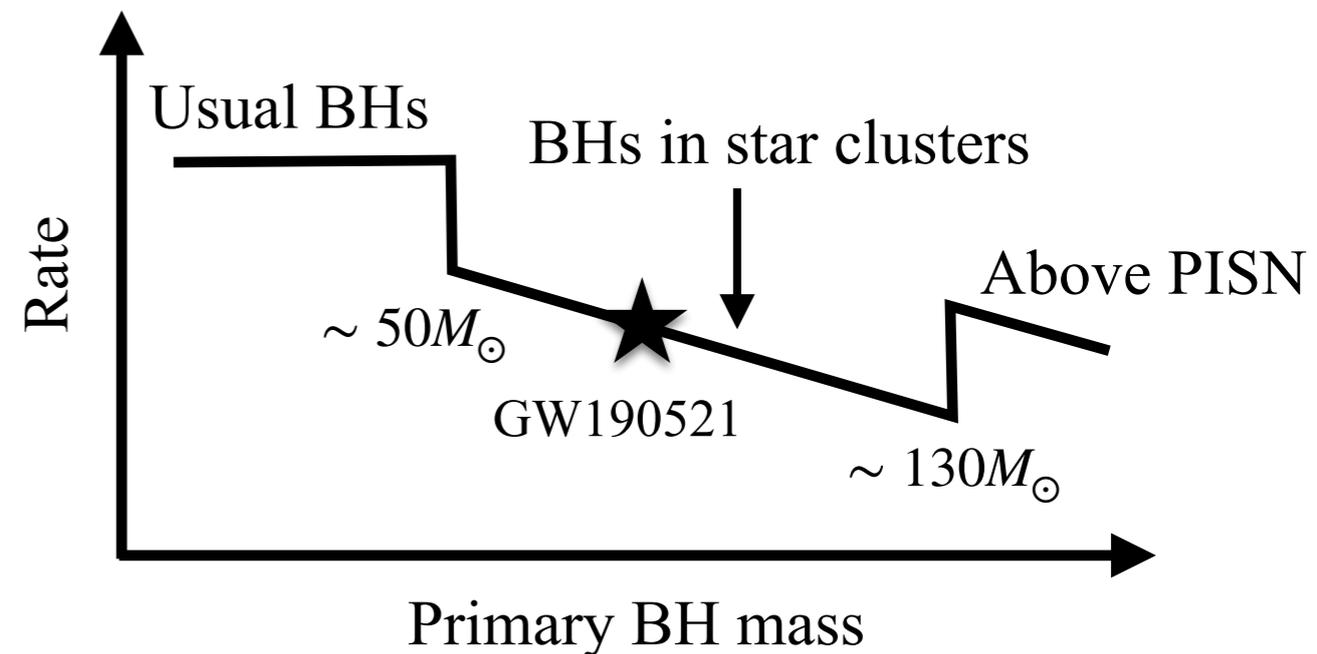
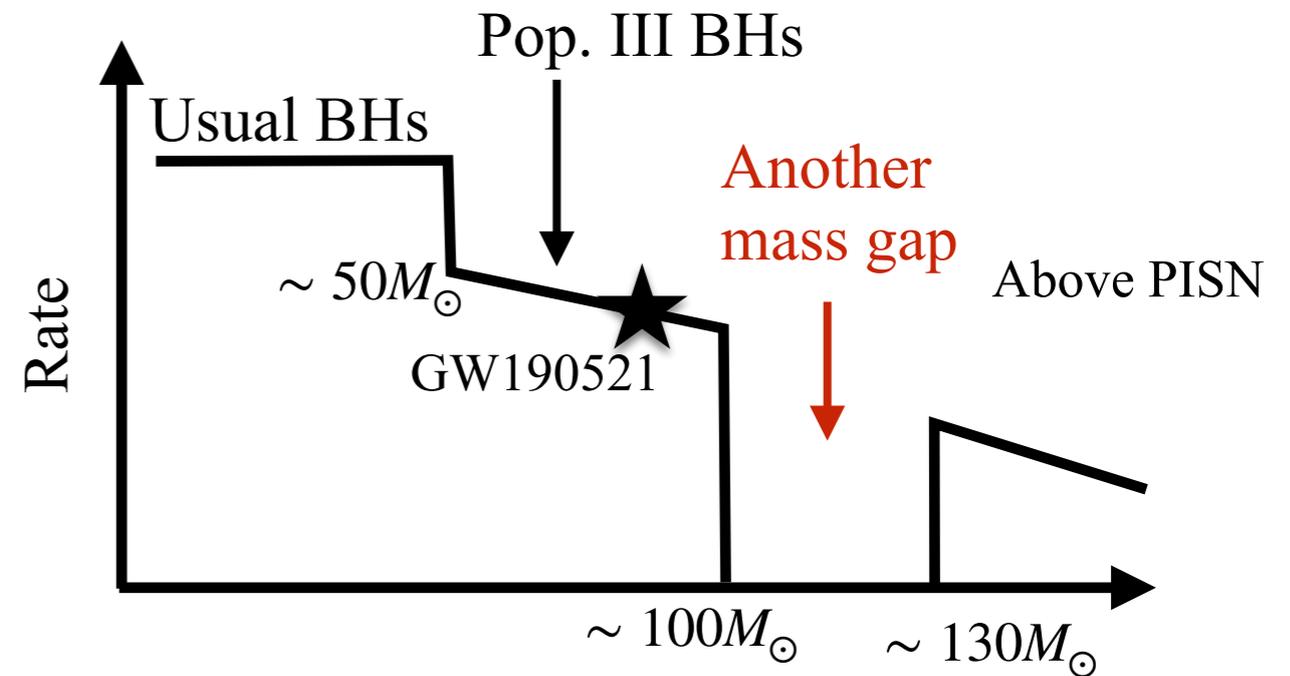
Pop III stars can form the PI mass-gap event if overshoot is ineffective.



Tanikawa et al. (2021, MNRAS, 505, 2170)

Difference from cluster origin

- Even if the M model is correct, no Pop. III binary can form BH-BHs with $100 - 130M_{\odot}$.
- If GW190521 is Pop. III, the merger rate of BH-BHs with $100 - 130M_{\odot}$ is much smaller than with $50 - 100M_{\odot}$.



Expectations for O4

- After June 2022
- Improved sky localization because of KAGRA joining
 - Electromagnetic counterparts?
- More many BH mergers discovered
 - The presence of $100 - 130M_{\odot}$ mass gap
 - Intermediate mass BH ($\gtrsim 100M_{\odot}$) mergers

Summary

- The origins of BH mergers have been under debate.
- Open clusters can be a promising formation site of merging BH mergers.
- Pop III stars can form the PI mass-gap event GW190521 if convective overshoot is not effective.